

BASIC ELECTRICAL & ELECTRONICS

Semester: 1st/2nd

STUDY MATERIAL



BASIC ELECTRICAL & ELECTRONICS

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Electrical energy :-

- It is a form of energy resulting from the flow of electric charge.
- Energy is the ability to do work, or apply force to move an object.

* Electrical energy is easy to use :-

conventional form :-

It can be converted from one form of energy into another form.

Easy to control :-

It can be easily controlled by turning on/off through switch.

Greater flexibility :-

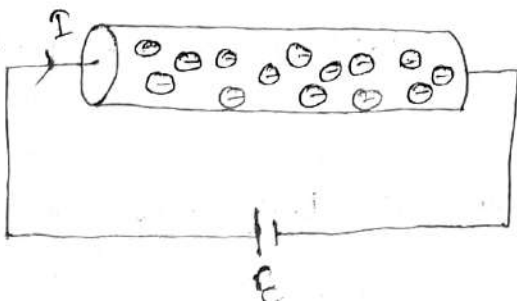
It can be transferred from one place to another place.

Cleanliness :-

It is not associated with any sources or any poisonous gases.

High Transmission efficiency :-

It has highly transmission efficiency.

Electric current :-

Matter \rightarrow Atoms \rightarrow Electrons, protons, Neutrons

$$q_e = -1.607 \times 10^{-19} \text{ C.}$$

$$q_p = 1.607 \times 10^{-19} \text{ C.}$$

The rate of flow of electric charges with respect to time is called electric current.

$$I = \frac{q}{t} \text{ or } \frac{dq}{dt}$$

unit \rightarrow Ampere.

Electric potential or voltages

The ability or the capacity of the charged body to do work is called electric potential.

$$\text{voltage (V)} = \frac{\text{work done}}{\text{charge}} = \frac{W}{q}$$

unit \rightarrow volt.

\rightarrow The virtue by which work can possibly done due to accumulation of electric charges is called electric potential.

(i) - If two points do not have same potential, then the difference of potential exist betw the two points which is called potential difference.

Electric power:

\rightarrow Power of device is defined as the rate of doing work.

\rightarrow Electric power refers to the rating of an electric

device and is defined as the rate at which the device can transform electrical energy into other forms of energy, such as mechanical energy, in heat energy and light energy.

$$P = \frac{W}{t}$$

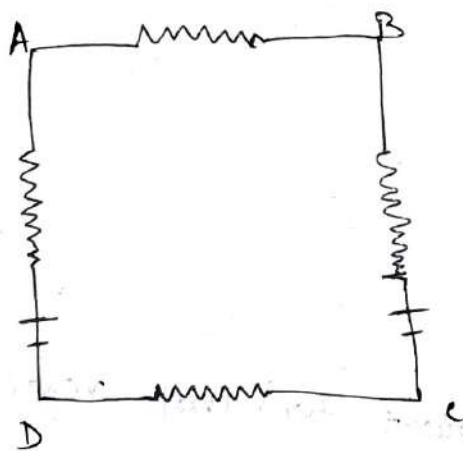
$$\Rightarrow \frac{dW}{dt}$$

$$P = VI.$$

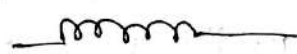
for resistance circuit $P = I^2 R.$


Circuit:-

A circuit is a closed conducting path through which an electric current flows.

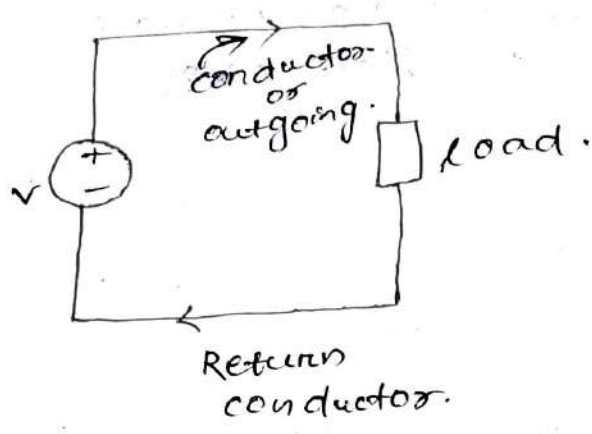


Resistance (R) — 

Inductance (L) — 

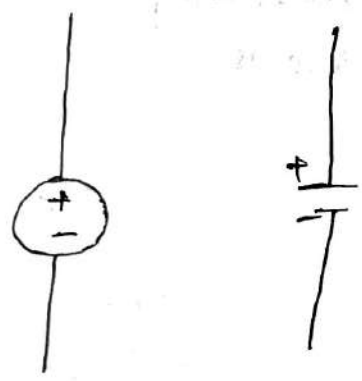
capacitance (C) — 

Source and load:-



- (1) - Source \rightarrow produces energy
- (2) - Load - utilises energy
- (3) - conductors.

Ideal voltage source:-



(symbols).

It maintains constant terminal voltage irrespective of variations in load ~~and~~ current.

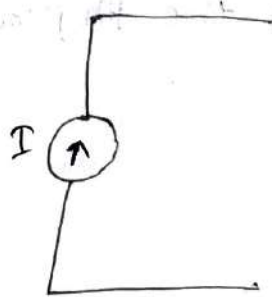
Internal resistance is present.

A voltage source in which the internal resistance is not zero is treated as a practical voltage source.

When a load is connected across the voltage source the terminal voltage doesn't remain equal to the emf of the source.

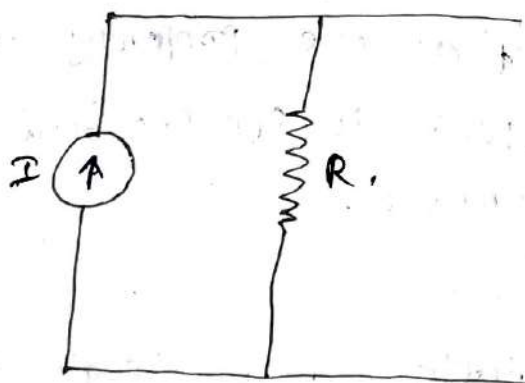
3.22
mathematically $V - iR = E$.

Ideal current source :-



(symbol).

Practical current source :-



(symbol).

→ A current source that maintains constant output current, irrespective of variations in load is called ideal current source.

→ A current source in which the internal resistance has a finite value is treated as

practical current source.

→ In practical current source output current may change with variations in load condition.

Ohm's Law:-

It states that "the voltage across an element is directly proportional to the current flowing through it, provided the physical conditions remains the same."

mathematically

$$V \propto I$$
$$\boxed{V = IR}$$

Symbol of (R) = Ω

R = Resistance.

Resistance:-

It may be defined as the property of a substance due to which it opposes the flow of electric current.

Property:-

- (1) - It varies directly as its length of conductor.
- (2) - It varies inversely as its cross-sectional area of conductor.
- (3) - It depends on nature of material.
- (4) - It also depends on the temperature of the conductor.

In mathematically,

$$R \propto l$$

$$R \propto \frac{1}{A}$$

$$R \propto \frac{l}{A}$$

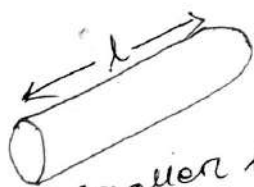
$$R = \rho \frac{l}{A}$$

ρ = specific resistance
or Resistivity.

$$\rho = \frac{AR}{l}$$

$$\text{unit} = \frac{\text{m}^2 \text{ohm}}{\text{m}} = \text{ohm m} = \Omega \text{m}.$$

Dt 26.3.22



smaller l

(a) - length.

(a) - larger area.

(i) - Low Resistance



larger l ,

(b) - smaller area.

(ii) - high resistance.

$$R \propto \frac{l}{A}$$

$$A \uparrow R \downarrow$$

$$A \downarrow R \uparrow$$

(iv) - R_0 at 0°C .

\downarrow

R_t at $t^\circ \text{C}$.

change in resistance = $R_t - R_0$.

$$R_t - R_0 \propto R_0$$

$$R_t - R_0 \propto t$$

$$R_t - R_0 \propto R_0 t$$

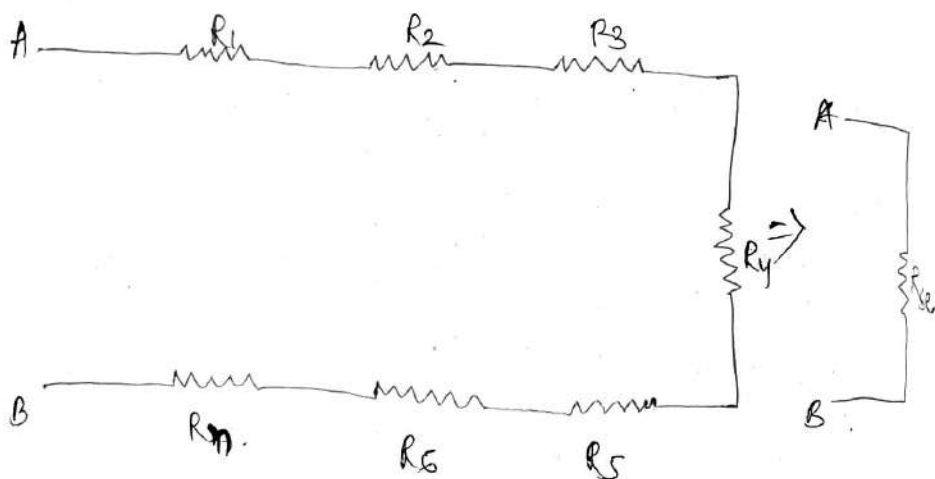
$$R_t - R_0 = \alpha R_0 t$$

$$R_t = R_0 + \alpha R_0 t$$

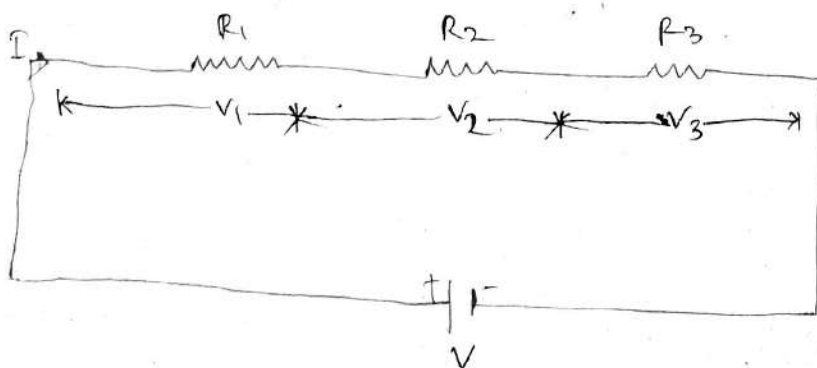
$$\Rightarrow R_t = R_0 (1 + \alpha t)$$

α = temperature coefficient of resistance

Resistance in series:-



$$R_{se} = R_1 + R_2 + R_3 + \dots + R_n$$



$$V = V_1 + V_2 + V_3$$

$$V = V_1 + V_2 + V_3$$

$$\Rightarrow IR = IR_1 + IR_2 + IR_3$$

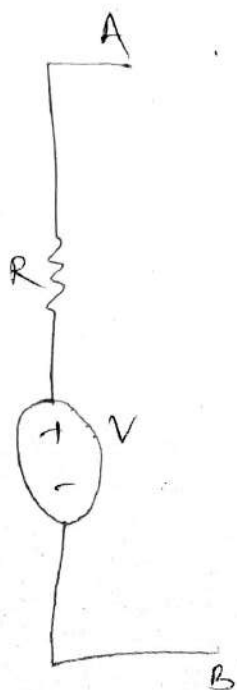
$$\Rightarrow IR = I(R_1 + R_2 + R_3)$$

$$\Rightarrow \boxed{R = R_1 + R_2 + R_3}$$

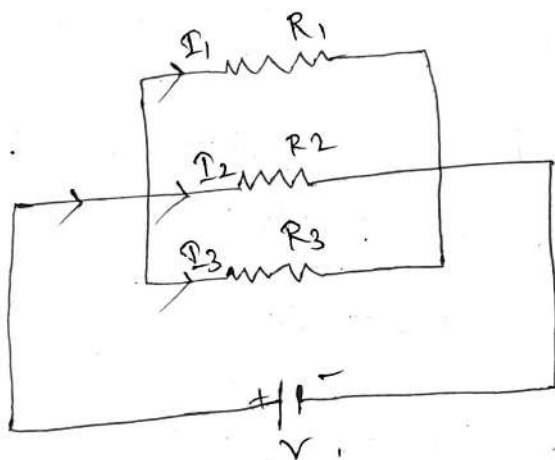
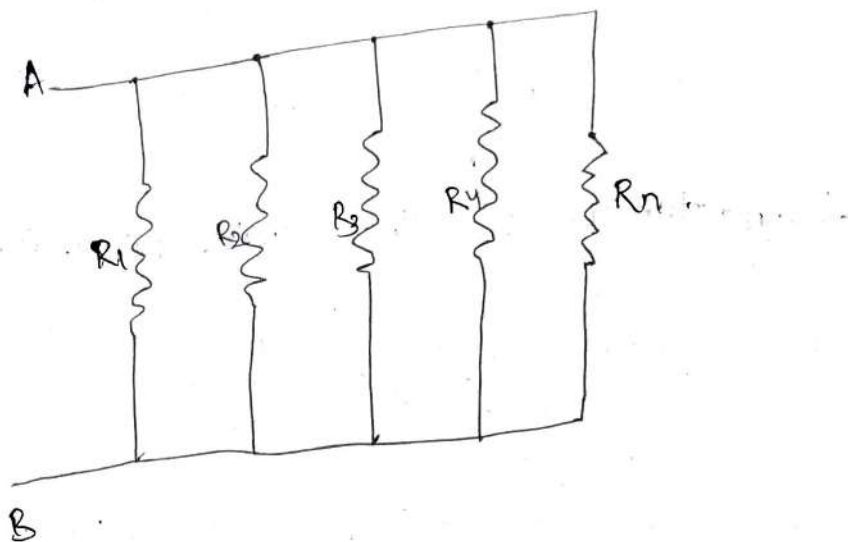
Main characteristics of series circuit:-

- (1)- same current flows through all the parts of a circuit.
- (2)- different resistances have their individual voltage drop.
- (3)- voltage drops are additive.
- (4)- Resistances are additive.
- (5)- power are additive.

Practical voltage source



Parallel circuit:-



$$I = I_1 + I_2 + I_3.$$

$$V = IR.$$

$$I = \frac{V}{R}$$

$$\frac{V}{R} = \frac{V}{R_1} + \frac{V}{R_2} + \frac{V}{R_3}.$$

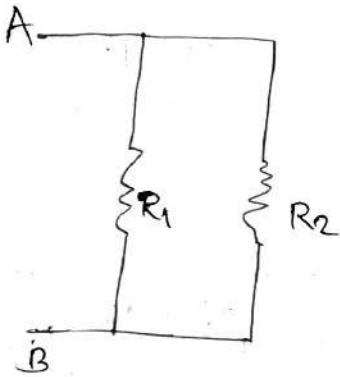
$$\Rightarrow \frac{V}{R} = V \left(\frac{1}{R_1} + \frac{1}{R_2} + \frac{1}{R_3} \right).$$

$$\Rightarrow \frac{1}{R} = \frac{1}{R_1} + \frac{1}{R_2} + \frac{1}{R_3}.$$

$$G_n = G_1 + G_2 + G_3$$

Characteristics of parallel circuit :-

- (1) - Same voltage acts through all the parts of a circuit.
- (2) - Different resistance have their individual current.
- (3) - currents are additive.
- (4) - conductances are additive.
- (5) - powers are additive.

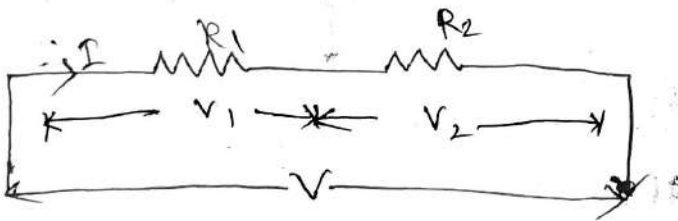


$$\frac{1}{R_p} = \frac{1}{R_1} + \frac{1}{R_2}$$

$$\Rightarrow \frac{1}{R_p} = \frac{R_2 + R_1}{R_1 R_2}$$

$$\Rightarrow \boxed{R_p = \frac{R_1 R_2}{R_1 + R_2}}$$

voltage divider equation :-



$$V_{eq} \text{ or } R_s = R_1 + R_2$$

$$I = \frac{V}{R_s}$$

$$V = IR_1$$

$$= \frac{V}{R_1 + R_2} \times R_1 \quad I = \frac{V}{R_1 + R_2} \quad \text{--- (1)}$$

$$\Rightarrow \boxed{V_1 = V \times \frac{R_1}{R_1 + R_2}}$$

Similarly

$$V_2 = IR_2$$

$$I = \frac{V}{R_1 + R_2} \times R_2$$

$$V_2 = V \times \frac{R_2}{R_1 + R_2}$$

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Current Divider Equations:-

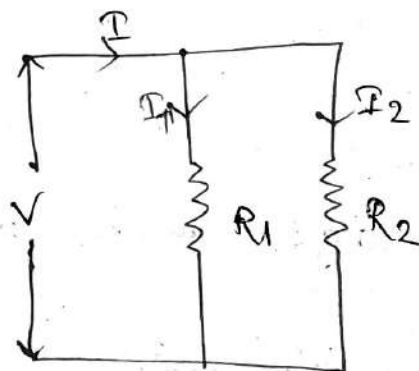
Let R_p = Total Resistance of the circuit.

I = Total current.

$$\frac{1}{R_p} = \frac{1}{R_1} + \frac{1}{R_2}$$

$$\Rightarrow \frac{1}{R_p} = \frac{R_2 + R_1}{R_1 R_2}$$

$$2) R_p = \frac{R_1 R_2}{R_1 + R_2} \quad \text{--- (1)}$$



$$I = \frac{V}{R_p}$$

Similarly, $I_1 = \frac{V}{R_1} \quad \text{--- (2)}$

$$I_2 = \frac{V}{R_2} \quad \text{--- (3)}$$

eqn (2) / eqn (1)

$$\frac{I_1}{I} = \frac{\frac{V}{R_1}}{\frac{V}{R_P}}$$

$$\Rightarrow \frac{I_1}{I} = \cancel{\frac{R_1}{R_P}} \times \frac{R_P}{V}$$

$$\Rightarrow \frac{I_1}{I} = \frac{R_P}{R_1}$$

$$\Rightarrow \frac{I_1}{I} = \frac{\frac{R_1 R_2}{R_1 + R_2}}{R_1}$$

$$\Rightarrow \boxed{\frac{I_1}{I} = \frac{R_2}{R_1 + R_2}}$$

$$\Rightarrow \boxed{I_1 = \frac{I R_2}{R_1 + R_2}}$$

similarly eqn (3) / eqn (1)

$$\frac{I_2}{I} = \frac{\frac{V}{R_2}}{\frac{V}{R_P}}$$

$$\Rightarrow \frac{I_2}{I} = \frac{R_P}{R_2}$$

$$\Rightarrow I_2 = \cancel{R_2} I \frac{R_1 R_2}{R_1 R_2} \frac{1}{R_2}$$

$$\Rightarrow \boxed{I_2 = \frac{I \cancel{R_1}}{R_1 + R_2}}$$

(Q) :- 3 resistors of value 3Ω , 8Ω & 24Ω are connected in parallel across a 12V DC supply. calculate

- (i) - The total resistance of the combination
- (ii) - The current in each branch.
- (iii) - The total current.

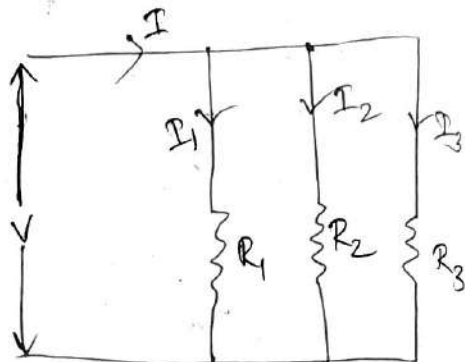
Ans.

~~Total resistance~~
Given, voltage = 12V .

$$R_1 = 3\Omega$$

$$R_2 = 8\Omega$$

$$R_3 = 24\Omega$$



$$\frac{1}{R_p} = \frac{1}{R_1} + \frac{1}{R_2} + \frac{1}{R_3}$$

$$\Rightarrow \frac{1}{R_p} = \frac{1}{3} + \frac{1}{8} + \frac{1}{24}$$

$$\Rightarrow \frac{1}{R_p} = \frac{8+3+1}{24} = \frac{1}{2}$$

$$\Rightarrow R_p = 2\Omega$$

$$I_1 = \frac{V}{R_1} = \frac{12}{3} = 4\text{ Amp.}$$

$$I_2 = \frac{V}{R_2} = \frac{12}{8} = \frac{3}{2} \text{ Amp.} = 1.5\text{ Amp.}$$

$$I_3 = \frac{V}{R_3} = \frac{12}{24} = \frac{1}{2} = 0.5 \text{ Amp.}$$

$$I = I_1 + I_2 + I_3$$

$$= 4 + 1.5 + 0.5$$

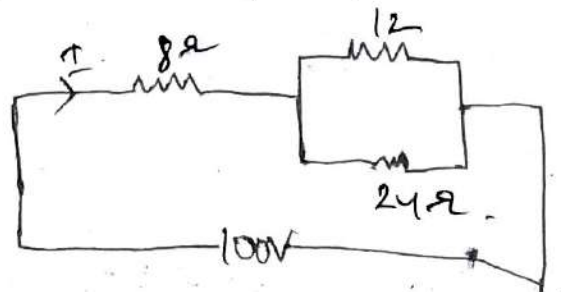
$$= 4 + \frac{15}{10} + \frac{5}{10}$$

$$= \frac{40 + 15 + 5}{10} = \frac{60}{10} = 6 \text{ Amp.}$$

Q. A Resistor of 8Ω is connected in series with a combination of 12Ω & 24Ω in parallel. The whole circuit is connected across 100V supply. Find

- (i) - The current taken from the supply.
- (ii) - The voltage across 8Ω ~~resistor~~ ^{resistor}.
- (iii) - current flowing in 12Ω & 24Ω resistors.

Ans: - $R_1 = 8\Omega$
 $R_2 = 12\Omega$
 $R_3 = 24\Omega$



$$\frac{1}{R_p} = \frac{1}{R_2} + \frac{1}{R_3}$$

$$\Rightarrow \frac{1}{R_p} = \frac{1}{12} + \frac{1}{24}$$

$$= \frac{2+1}{24} = \frac{3}{24}$$

$$\Rightarrow R_p = 8 \Omega$$

$$R_{eq} = R_1 + R_p$$

$$\Rightarrow R_{eq} = 8 + 8 \\ = 16 \Omega$$

~~The voltage across is~~

$$(ii) \text{ Current } I = \frac{V}{R_{eq}}$$

$$= \frac{100}{16} = 6.25 \text{ Ampere}$$

i) The voltage across 8Ω

$$V_1 = IR_1$$

$$= 6.25 \times 8$$

$$= 50 \text{ volt.}$$

ii) current flowing in 12Ω & 24Ω

$$R_{eq} = 16\Omega$$

$$I_2 = \frac{V}{R_2} \text{ or } I \times \frac{R_3}{R_2 + R_3}$$

$$= \frac{50}{12} = 4.26 \text{ Amp.}$$

$$I_3 = \frac{V}{R_3} \text{ or } I \times \frac{R_2}{R_2 + R_3}$$

$$= \frac{50}{24} = 2.08 \text{ Amp.}$$

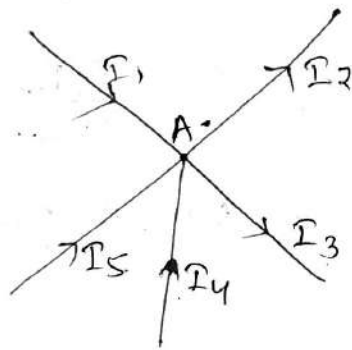
Kirchhoff's laws:

- (1) - Kirchhoff's current law (KCL)
- (2) - Kirchhoff's voltage law (KVL)

(1) - Kirchhoff's current law (KCL):

→ It states that "In a circuit at any given junction the algebraic sum of currents meeting at a point is zero".

$$\sum_{j=1}^n I_j = 0.$$



Incoming current (+ve)

Outgoing current (-ve).

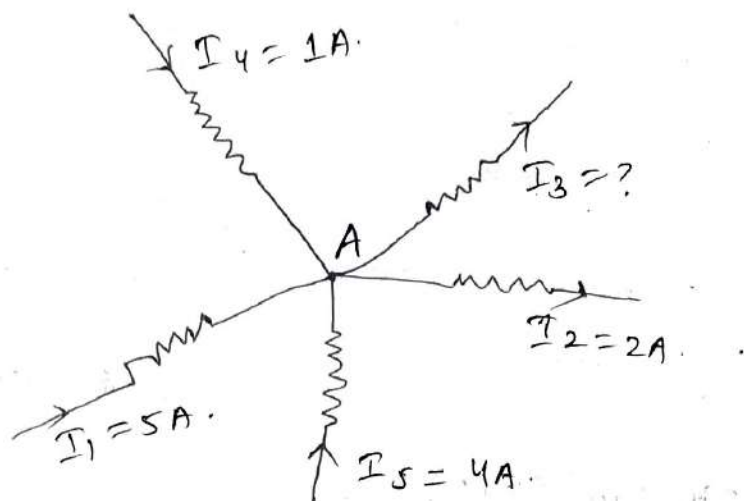
$$I_1 + (-I_2) + (-I_3) + I_4 + I_5 = 0.$$

$$\Rightarrow I_1 - I_2 - I_3 + I_4 + I_5 = 0.$$

$$\Rightarrow I_1 + I_4 + I_5 = I_2 + I_3.$$

Total incoming current = Total outgoing current

q):



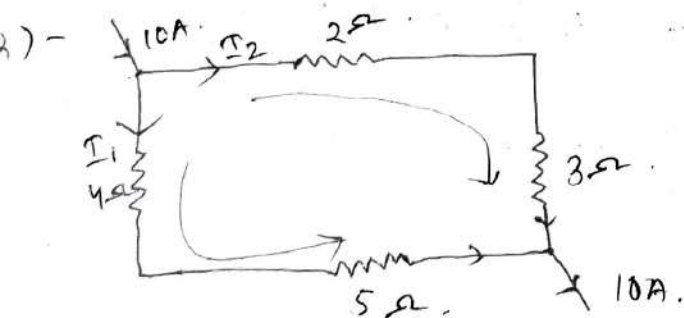
Find the value of I_3 .

Applying KCL to node A.

$$I_1 + I_2 - I_3 + I_4 + I_5 = 0.$$

$$\Rightarrow 5A - 2A - I_3 + 1A + 4A = 0.$$

$$\Rightarrow I_3 = 8A. \quad (\text{Ans})$$

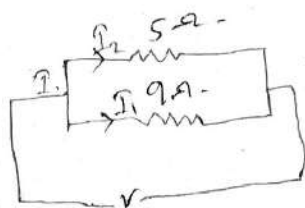


Find the values of I_1 and I_2 shown in figure by applying KCL.

$$I_1 = I \times \frac{5}{9+5}$$

$$\Rightarrow I_1 = 10 \times \frac{5}{14}$$

$$\Rightarrow I_1 = 3.57A$$



$$I = I_1 + I_2$$

$$\Rightarrow 10 = 3.57 + I_2$$

$$\Rightarrow I_2 = 10 - 3.57$$

$$\Rightarrow I_2 = 6.43 \text{ A}$$

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(2) Kirchhoff's voltage law (KVL) :-

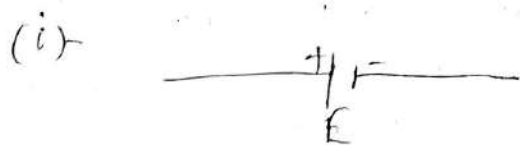
Statement:- It states that "the algebraic sum of product of current and resistance in each of the conductors plus the algebraic sum of EMF in that path is zero".

$$\text{Mathematically } \sum IR + \sum EMF = 0$$

How to apply KVL in a circuit ?

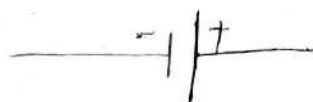
Determination of voltage sign :-

(i) sign of Battery :-



voltage drop $-E$

(ii) -



voltage gain $+E$

(2) - Sign of IR :-

(i) - $\xrightarrow{I} \overset{+}{\text{---} R \text{---}} \xrightarrow{\quad} \rightarrow \text{voltage drop } -IR.$

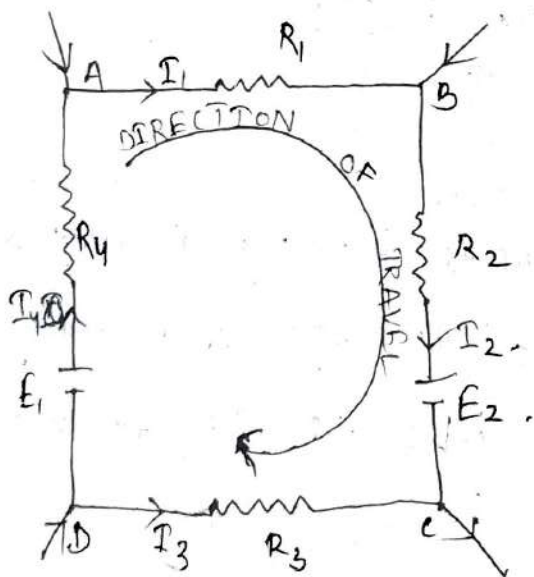
(ii) - $\xrightarrow{\quad} \overset{-}{\text{---} R \text{---}} \xleftarrow{I} \rightarrow \text{voltage gain } +IR.$

(iii) - $\xrightarrow{\quad} \overset{+}{\text{---} L \text{---}} \xrightarrow{\quad}$

$$V_L = -L \frac{dI}{dt} \quad (\text{voltage drop}).$$

(iv) - $\xrightarrow{\quad} \overset{-}{\text{---} L \text{---}} \xleftarrow{\quad}$

$$V_L = +L \frac{dI}{dt} \quad (\text{voltage gain}).$$



(1) - $I_1 R_1$ (voltage drop).

(2) - $I_2 R_2$ (voltage drop).

(3) - E_2 (voltage drop).

(4) - $I_3 R_3$ (voltage gain).

(5) - E_1 (voltage gain).

(6) - $I_4 R_4$ (voltage drop).

According to KVL,

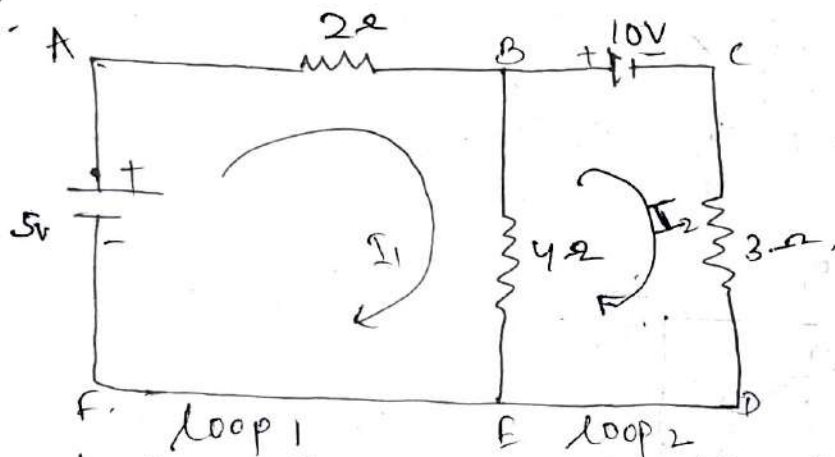
$$\sum IR + \sum EMF = 0.$$

$$\Rightarrow -I_1 R_1 - I_2 R_2 - E_2 + I_3 R_3 + E_1 - I_4 R_4 = 0.$$

$$\Rightarrow I_3 R_3 + E_1 = I_1 R_1 + I_2 R_2 + I_4 R_4 + E_2.$$

$$\Rightarrow E_1 - E_2 = I_1 R_1 + I_2 R_2 + I_4 R_4 - I_3 R_3.$$

(Q):



calculate the currents flowing in all the three resistances and voltage drop across 4Ω by applying KVL to the network?

In loop 1,

$$-2I_1 - 4(I_1 - I_2) + 5 = 0.$$

$$(I_1 > I_2).$$

In loop 2 $\Rightarrow -2I_1 - 4I_1 + 4I_2 + 5 = 0 \Rightarrow 4I_2 - 6I_1 + 5 = 0.$

$$-10 - 3I_2 - 4(I_2 - I_1) = 0.$$

$$\Rightarrow -10 - 3I_2 - 4I_2 + 4I_1 = 0 \Rightarrow 4I_1 - 7I_2 - 10 = 0.$$

According to KVL

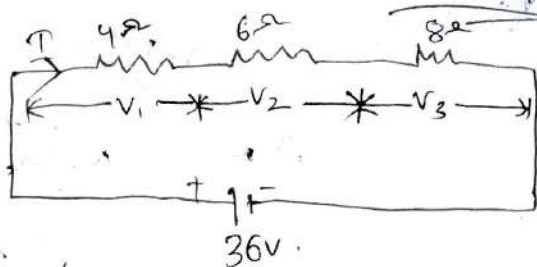
$$2I_1 - 4(I_1 - I_2) + 5 - 10 - 3I_2 - 4(I_2 - I_1)$$

$$\Rightarrow 4I_2 - 6I_1 + 4I_1 - 7I_2 = 10 - 5$$

$$\Rightarrow -2I_1 - 3I_2 = 5$$

$$\Rightarrow 2I_1 + 3I_2 = -5$$

(a):



$$R_1 = 4\Omega, R_2 = 6\Omega,$$

$$R_3 = 8\Omega.$$

Total resistance of

$$\text{the circuit } R_{se} = 4 + 6 + 8 = 18\Omega$$

$$\text{Total current } I = \frac{V}{R_{se}} = \frac{36}{18} = 2A$$

• Voltage drop across 4Ω

$$V_1 = IR_1$$

$$= 2 \times 4 = 8V.$$

$$\text{across } 6\Omega \Rightarrow V_2 = IR_2 = 2 \times 6 = 12V.$$

$$\text{across } 8\Omega \Rightarrow V_3 = IR_3 = 2 \times 8 = 16V.$$

$$V = V_1 + V_2 + V_3$$

$$= 8 + 12 + 16 = 36V.$$

Power consumed in 4Ω

$$P_1 = I^2 R_1 = 2^2 \times 4 = 16W.$$

$$P_2 = I^2 R_2 = 2^2 \times 6 = 24W.$$

$$P_3 = I^2 R_3 = 2^2 \times 8 = 32W.$$

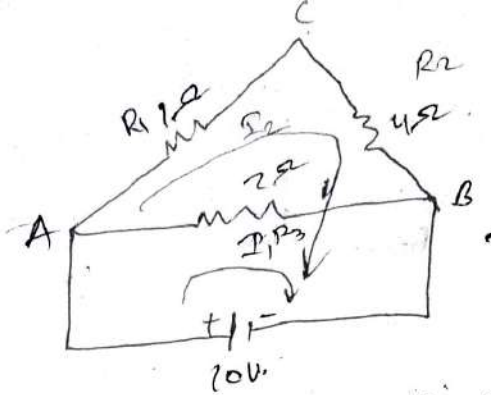
$$P = P_1 + P_2 + P_3$$

$$= 16 + 24 + 32 = 72W.$$

$$\text{or } P = VI = 36 \times 2 = 72W$$

(Ans)

(a) :



calculate the currents flowing in all the three resistances and total current supplied by the 10V battery by applying KVL to the network.

Ans:- $\sum IR = 0$

$\sum IR = 0$

Loop-1

$$10 - I_1 R_3 = 0$$

$$\Rightarrow 10 - I_1 \times 2 = 0$$

$$\Rightarrow -2I_1 = -10$$

$$\Rightarrow I_1 = 0.5A$$

Loop-2

$$10 - I_2 = 0 \quad 10 - I_2 - 4I_2 = 0$$

$$\Rightarrow I_2 = 10 \quad \Rightarrow 10 - 5I_2 = 0$$

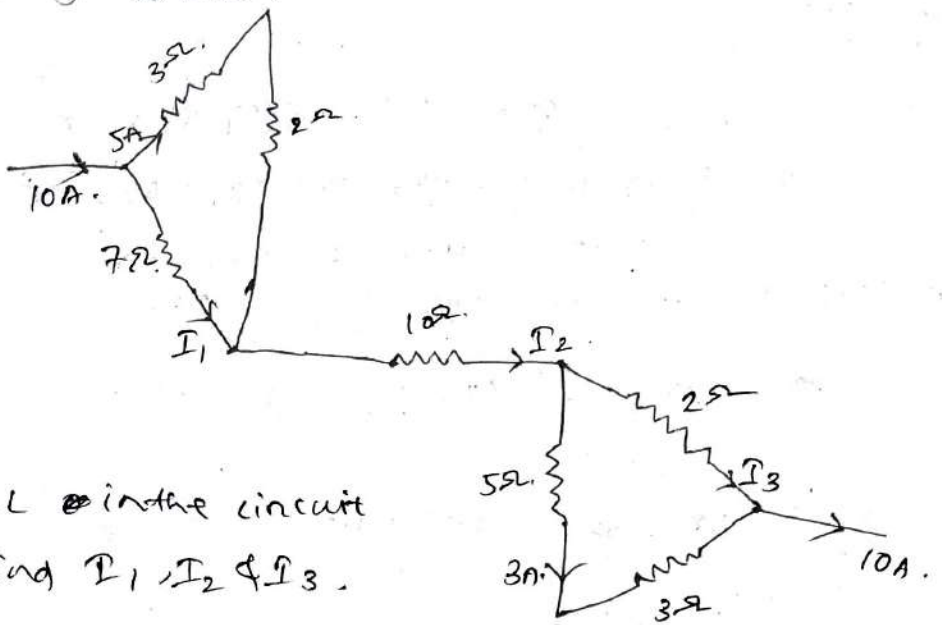
$$10 - I_2 \times 4 = 0 \quad \Rightarrow -5I_2 = -10$$

$$\Rightarrow 4I_2 = 10 \quad \Rightarrow I_2 = 2.5A$$

$$\Rightarrow I_2 = \frac{5}{2} = 2.5A$$

According to KVL

Q 1:-



Apply KCL in the circuit and find I_1 , I_2 & I_3 .

Ans:- $i = i_1 + i_2$

$\Rightarrow 10 = i_1 + 5$

$\Rightarrow i_1 = 10 - 5 = 5A$

$I_2 = 10A$

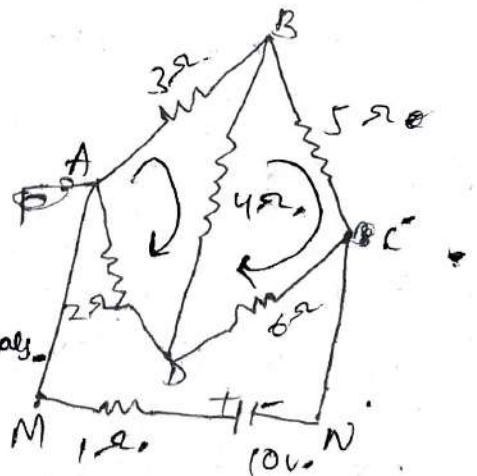
~~I_2~~ $I_2 = I_3 + 3A$

$I_3 = 10 - 3 = 7A$

Q2:- Applied KVL and determine

(i) - current in each resistance.

(ii) - voltage drop across terminals B and D.



In loop-1

$$10 - I_1 - 2(I_1 - I_2) - 6(I_1 - I_3) = 0$$

$$\Rightarrow 10 - I_1 - 2I_1 + 2I_2 - 6I_1 + 6I_3 = 0$$

in loop-2

$$2I_2 + 6I_3 - 9I_1 + 10 = 0 \quad \text{--- (1)}$$

$$\Rightarrow 9I_1 - 2I_2 - 6I_3 = 10$$

$$10 - 3I_2 - 4(I_2 - I_3) - 2(I_2 - I_1) = 0$$

$$\Rightarrow 10 - 3I_2 - 4I_2 + 4I_3 - 2I_2 + 2I_1 = 0$$

$$2I_1 - 9I_2 + 4I_3 = 0$$

$$\Rightarrow 2I_1 - 9I_2 - 4I_3 = 0 \quad \text{--- (2)}$$

in loop-3

$$10 - 5I_3 - 6(I_3 - I_1) - 4(I_3 - I_2) = 0$$

$$\Rightarrow 10 - 5I_3 - 6I_3 + 6I_1 - 4I_3 + 4I_2 = 0$$

$$\Rightarrow 6I_1 + 4I_2 - 15I_3 = 0 \quad \text{--- (3)}$$

According to KVL:2I₂

add eqn (1), (2) & (3).

$$2I_2 + 6I_3 - 9I_1 + 10 + 2I_1 - 9I_2 - 4I_3 + 6I_1 + 4I_2 - 15I_3 = 0$$

$$\Rightarrow -3I_2 - 13I_3 - I_1 + 10 = 0$$

$$\Delta = \begin{vmatrix} 9 & -2 & -6 \\ 2 & -9 & 4 \\ 6 & 4 & -15 \end{vmatrix}$$

$$= 9(135 - 16) + 2(-30 - 24) - 6(8 + 54).$$

$$= \overset{119}{\cancel{154}} \times 9 + 2 \times (-54) - 62 \times 6.$$

$$= 1071 - 108 - 372$$

$$= 591.$$

$$\Delta I_1 = \begin{vmatrix} 10 & -2 & -6 \\ 0 & -9 & 4 \\ 0 & 4 & -15 \end{vmatrix} = 10 \times (135 - 16) = 10 \times 119 = 1190.$$

$$\Delta I_2 = \begin{vmatrix} 9 & 10 & -6 \\ 2 & 0 & 4 \\ 6 & 0 & -15 \end{vmatrix} = 10 \times (-30 - 24) = 10 \times (-54) = -540.$$

$$\Delta I_3 = \begin{vmatrix} 9 & -2 & 10 \\ 2 & -9 & 0 \\ 6 & 4 & 0 \end{vmatrix} = 10 \times (8 + 54) = 620.$$

$$\textcircled{1} \quad I_1 = \frac{\Delta I_1}{\Delta} = \frac{1190}{591} = 2.01 \text{ A}.$$

$$I_2 = \frac{\Delta I_2}{\Delta} = \frac{-540}{591} = -0.913 \text{ A}.$$

$$I_3 = \frac{\Delta I_3}{\Delta} = \frac{620}{591} = 1.049 \text{ A}.$$

$$(2) \quad V_{BD} = I_{BD} \cdot R_{BD} \quad (I_{BD} = I_3 - I_2 = 1.05 - 0.913 = 0.137)$$

$$= 0.137 \times 4$$

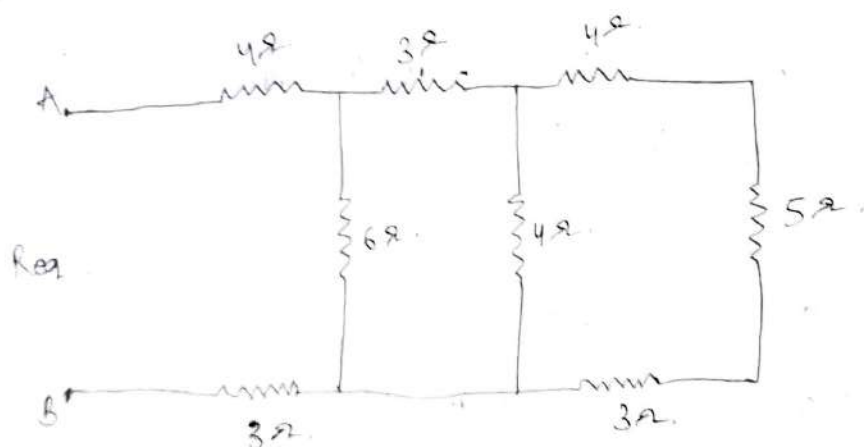
$$= 0.548 \text{ V} \quad (\text{Ans})$$

DT 6.5.22

Equivalent Resistance:-

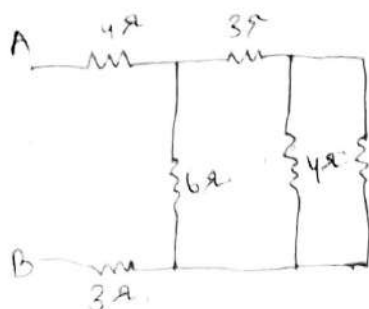
Equivalent resistance of a circuit or network between its any two points is given by that single resistance which can replace the entire circuit between that points.

(Q):



Ans:

(1)-

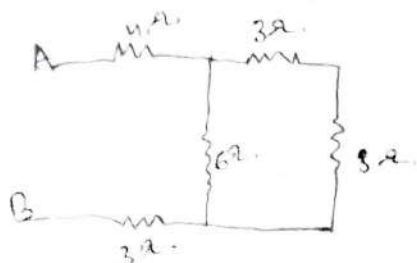


$$R_{eq} = 4 + 5 + 3 = 12 \Omega$$

$$R_p = \frac{R_1 R_2}{R_1 + R_2} = \frac{4 \times 12}{4 + 12}$$

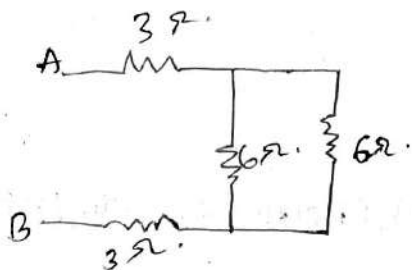
$$= \frac{48}{16} = 3 \Omega$$

(2)



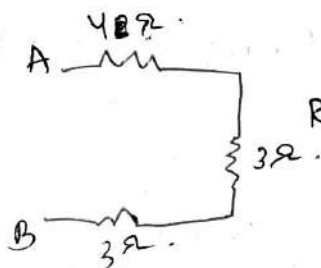
$$3 \Omega + 3 \Omega = 6 \Omega$$

③

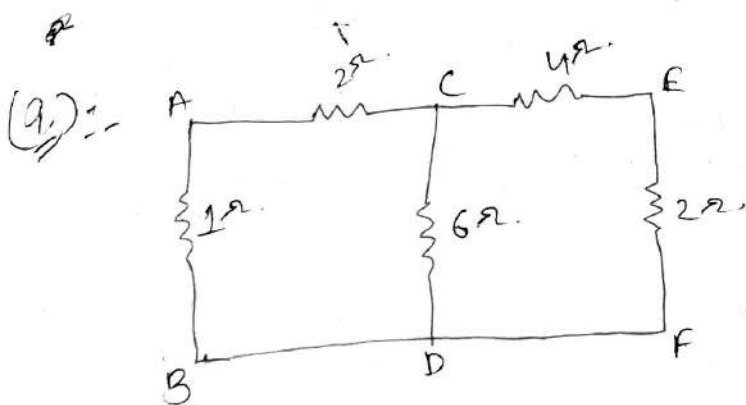


$$R_p = \frac{R_1 R_2}{R_1 + R_2} = \frac{6 \times 6}{6 + 6} = \frac{36}{12} = 3\Omega$$

④

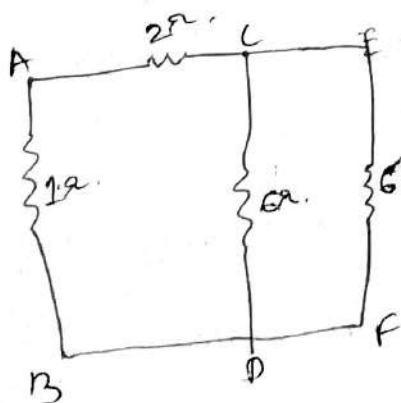


$$R_{eq} = 4 + 3 + 3 = 10\Omega$$

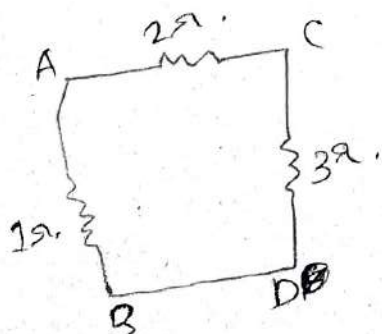


Ans! :-

① $4\Omega + 2\Omega = 6\Omega$



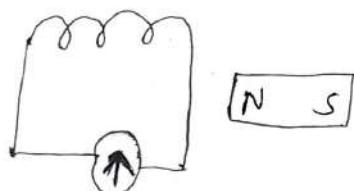
$$R_p = \frac{6 \times 6}{6 + 6} = 3\Omega$$



$$R_{eq} = 2 + 3 + 1 = 6\Omega$$

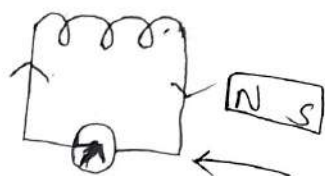
Electromagnetic Induction:-

Definition:- It is the phenomenon of producing induced current in a closed circuit due to change in magnetic field around it.



(Magnet is at rest)

(i)



(Magnet is moving towards the coil)

(ii)

Faraday's 1st law:-

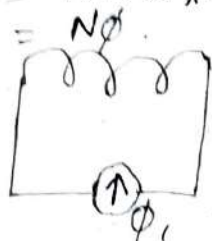
It states that "whenever the magnetic flux linked with a circuit changes an emf is induced in it".

or :- It states that "whenever a conductor cuts magnetic flux an emf is induced in it".

Faraday's 2nd law:-

It states that "The magnitude of the induced emf is equal to the rate of change of flux linkages".

→ Flux linkages = NO. of turns \times flux.



• Initial flux linkages = $N \times \Phi_1$

$$= N\Phi_1$$

final flux linkages = $N\Phi_2$

$$\text{Induced EMF } (e) = \frac{N\Phi_2 - N\Phi_1}{t}$$

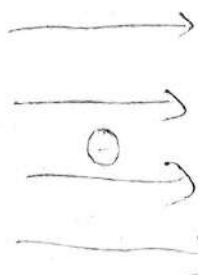
$$= N \frac{\Phi_2 - \Phi_1}{t}$$

$$e = -N \frac{d\Phi}{dt}$$

Induced EMF \rightarrow $\begin{cases} \rightarrow \text{Dynamically Induced EMF.} \\ \rightarrow \text{Statically Induced EMF.} \end{cases}$

Dynamically Induced EMF:-

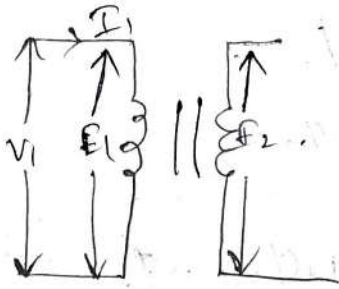
• when the magnetic field remains stationary but the conductor moves across it, then it is known as Dynamically Induced EMF.



$$e = Blv \sin \theta$$

1- Statically Induced Emf

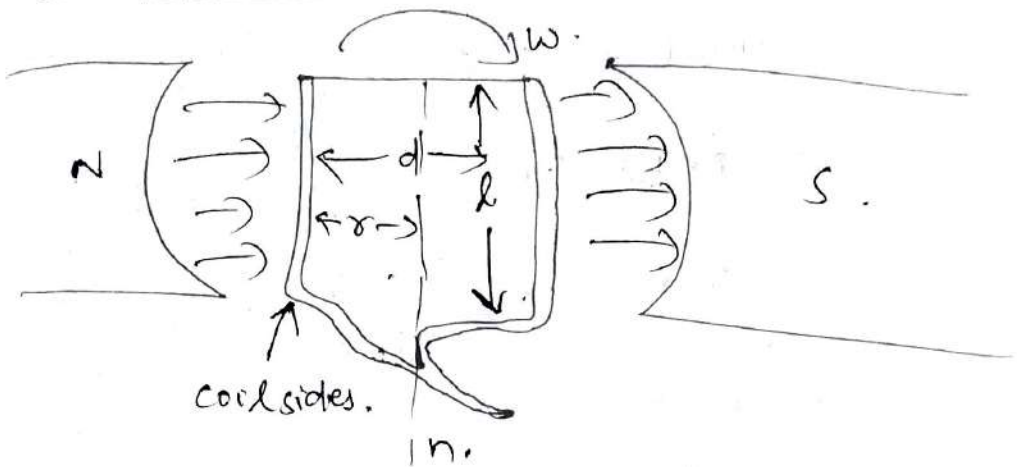
When the coils remain stationary, but flux through it ~~ex~~^{an} changes then it is known as statically Induced Emf.



As

Ac circuit

EMF Generation:

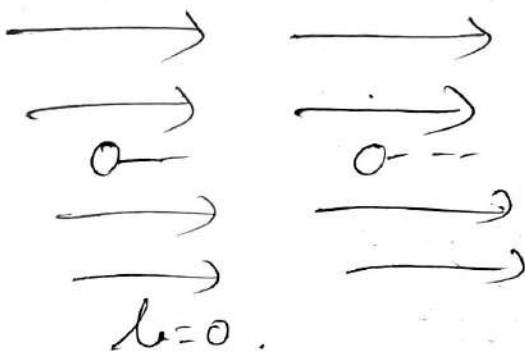


$$E = Blv \sin \theta.$$

B = magnetic flux density.

l = length of the conductor.

v = velocity of the conductor.



$$0^\circ < \theta < 90^\circ.$$

$$\omega = \text{Angular Velocity} = 2\pi n.$$

$$E = 2e$$

$$v = r\omega$$

~~ω = 2πn~~

$$\omega = 2\pi n$$

$$v = 2\pi r n.$$

$$E = 2e$$

$$e = 2Blv \sin \theta$$

$$= 2Bl (\omega r) \sin \theta$$

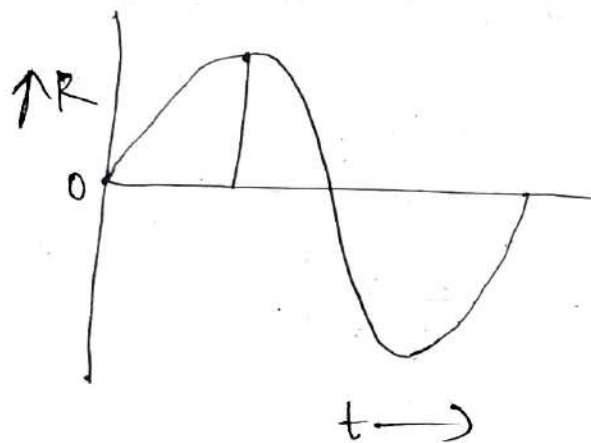
$$= 2\pi nBl (\omega r) \sin \theta$$

$$= 2\pi nB (lnd) \sin \theta$$

$$E = 2\pi nBA \sin \theta$$

$$\text{or } \boxed{E = E_n \sin \theta} \quad \text{or } \boxed{E = E_n \sin \omega t}$$

where $E_n = 2\pi nBA$



A single phase emf generation is based on the principle of dynamical induced emf. According to this principle a conductor of length l while moving with velocity v making an angle θ to a steady magnetic field of a

flux density (B) becomes the shaped as a dynamically induced EMF (\mathcal{E}) produced.

where $\boxed{\mathcal{E} = B l N \sin \theta}$.

It consist of a pair of magnetic force designated as north pole and south pole in the form of a permanent magnet with a coil placed in between which can freely rotate about an axis perpendicular to the direction of the magnetic field produce by the magnet. The magnetic field ~~is~~ has a flux density B in (weber/m²) W/m² in the space between the two pole which is assume to be uniform through out the space. The coil is formed by use of two conductors as the coil size.

Each conductor has an effective length of (l) in m. The separation between the conductor is taken as d . so the effective area of the ~~coil~~ coil becomes $A = l \times d$ in m².

The coil is mounted on a shaft. When the shaft is made to rotate at n revolution per second, it produces an angular speed of ω .

$$\omega = 2\pi n.$$

The e ends connected to a pair of isolated C-plings x and y , which form a kind of sliding contact with a pair of fixed carbon brushes

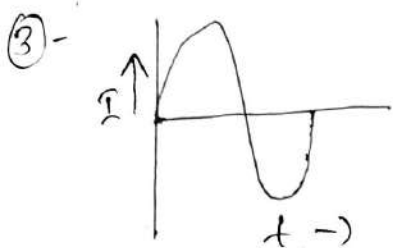
(b_1, b_2) for collection of the emf induced in the coil per external induce.

Difference betⁿ AC & DC :-

AC (2)

(1) Alternating current changes its magnitude and direction periodically.

(2) It is the graph betⁿ current and time.



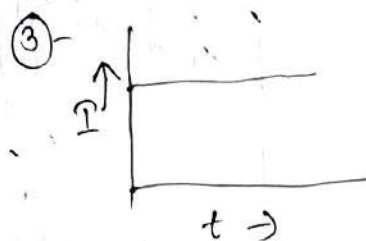
(4) AC can be generated at high voltages.

(5) With the help of Transformer generated voltage can be stepped up.

DC

(1) Direct current always flows in one dirⁿ.

(2) It is the graph betⁿ current and time.



(4) DC cannot be generated at high voltages.

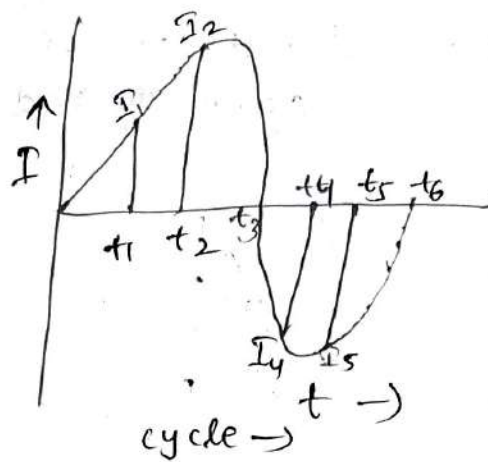
(5) But in DC use of Transformer is not possible.

Values of Alternating quantity :-

- (1) - Instantaneous value.
- (2) - Maximum or Peak value.
- (3) - Average or mean value.
- (4) - Effective or Root mean square value (RMS).

1. (1) - Instantaneous value:-

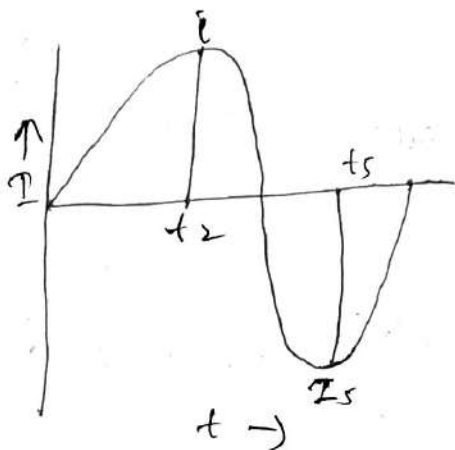
The value of alternating quantity at any given instant or time is called Instantaneous value.



| <u>Time (t)</u> | <u>Current (I)</u> |
|-----------------|--------------------|
| $t = 0$ | 0 |
| t_1 | i_1 |
| t_2 | i_2 |
| t_3 | 0 |
| t_4 | $-i_4$ |
| t_5 | $-i_5$ |

2. Maximum value or peak value:-

The maximum value attained by an alternating quantity is called maximum value or peak value.



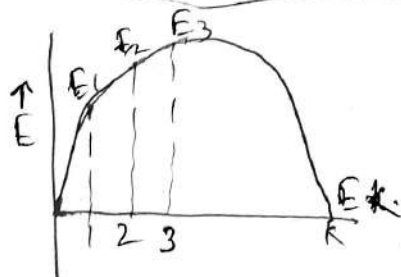
(3)- Average value :-

It gives the arithmetic mean of all instantaneous values over a given ~~period~~ period of time.

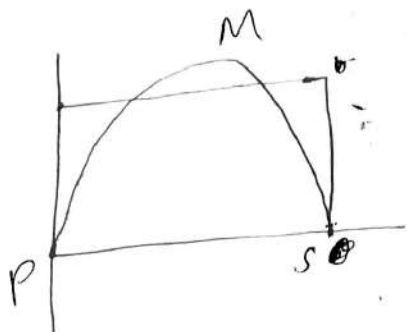
method :-

- (1)- Mid-ordinate method.
- (2) - Integration method.

① mid-ordinate method :-



$$E_{av} = \frac{E_1 + E_2 + E_3 + \dots + E_K}{K}$$

(2) - Integration method:

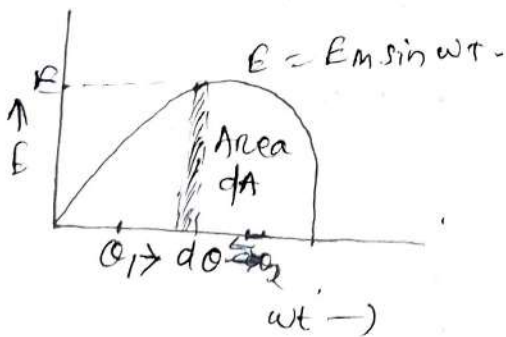
Rectangular Area = A

Average value = Height of rectangle.

Area of rectangle = Height \times Base.

$$\text{Average value of rectangle} = \text{Height} = \frac{\text{Area}}{\text{Base}}$$

$$= \frac{A}{P_S} \quad \text{--- (1)}$$



$$dA = E d\theta$$

$$= E_m \sin \theta d\theta$$

$$A = \int_{\theta_1}^{\theta_2} dA = \int_{\theta_1}^{\theta_2} E_m \sin \theta d\theta$$

$$= E_m \int_{\theta_1}^{\theta_2} \sin \theta d\theta$$

$$= -E_m (\cos \theta)$$

from eqn (1).

$$\text{Avg value} = \frac{A}{PS}$$

$$= \frac{-E_m [\cos \theta]_{\theta_1}^{\theta_2}}{PS}$$

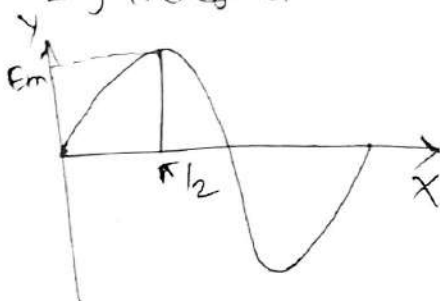
$$= \frac{-E_m [\cos \theta]_{\theta_1}^{\theta_2}}{\theta_2 - \theta_1}$$

$$= \frac{-E_m [\cos \theta_2 + \cos \theta_1]}{\theta_2 - \theta_1}$$

$$E_{\text{avg}} = \frac{E_m [\cos \theta_1 - \cos \theta_2]}{\theta_2 - \theta_1}$$

$$I_{\text{avg}} = \frac{I_m [\cos \theta_1 - \cos \theta_2]}{\theta_2 - \theta_1}$$

Q1):- calculate the average value of an emf sinusoid over the period 0 to $\frac{\pi}{2}$ by integration method.



$$\theta_1 = 0$$

~~Energy~~
$$\theta_2 = \frac{\pi}{2}$$

$$E_{avg} = \frac{E_m [\cos \theta_1 - \cos \theta_2]}{\theta_2 - \theta_1}$$

$$= E_m \left[\cos 0^\circ - \cos \frac{\pi}{2} \right]$$

~~$$\frac{0 - \frac{\pi}{2}}{\frac{\pi}{2} - 0}$$~~

$$= \frac{E_m [1 - 0]}{\frac{\pi}{2}}$$

$$= \frac{E_m}{\frac{\pi}{2}}$$

$$= \cancel{2E_m} \frac{2E_m}{\pi}$$

$$= \frac{2E_m}{\frac{\pi}{2}}$$

$$= \frac{14}{22} E_m$$

$$= \frac{7E_m}{11}$$

$$0.63$$

$$= 0.632 E_m$$

(Q1):- calculate the average value of sinusoid over the period $0 - 2\pi$.

Ans:- $\theta_1 = 0$
 $\theta_2 = 2\pi$

$$E_{avg} = \frac{E_m [\cos \theta_1 - \cos \theta_2]}{\theta_2 - \theta_1}$$

$$= \frac{E_m [\cos 0^\circ - \cos 2\pi]}{2\pi - 0}$$

$$= \frac{E_m [1 - 1]}{2\pi}$$

$$= \frac{0}{2\pi} = 0.$$

(Q2):- calculate the average value of an emf ~~sin~~ sinusoid over the period $0 - 2\pi$ by the integration method.

Ans:- $\theta_1 = 0$

$\theta_2 = \pi$

$$E_{avg} = \frac{E_m [\cos \theta_1 - \cos \theta_2]}{\theta_2 - \theta_1}$$

$$= \frac{E_m [\cos 0^\circ - \cos \pi]}{2\pi - 0}$$

$$= \frac{E_m [1 + 1]}{2\pi}$$

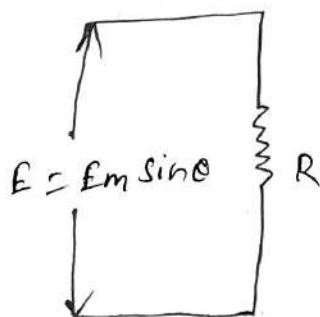
$$= \frac{2E_m}{2\pi} = \frac{E_m}{\pi}$$

$$= \frac{7}{22} E_m$$

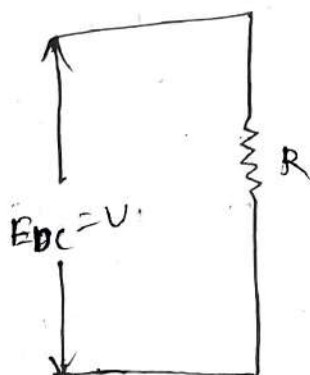
$$= 0.673 E_m$$

(4) - Effective value or Root Mean Square (R.M.S) value:-

Effective value of alternating quantity means finding the effectiveness of a given quantity over a specified period of time.



(i).



(ii).

in figure (i).

Power consumed over a period of time.

$$P = \frac{W}{t} \text{ or } \frac{dW}{dt}$$

$$\text{or } dW = P dt$$

$$W = \int_0^t P dt = \int_0^t \frac{E^2}{R} dt$$

$$= \int_0^t \frac{(E_m \sin \omega t)^2}{R} dt \quad \text{--- (1)}$$

figure (ii)

$$\begin{aligned} W_{dc} &= \int_0^t P dt = \int_0^t \frac{V^2}{R} dt = \frac{V^2}{R} \int_0^t dt \\ &= \frac{V^2}{R} t \quad \text{--- (2)} \end{aligned}$$

$$\omega_{dc} = \omega_{ac}$$

$$\Rightarrow \frac{V^2}{R} t = \int_0^t \frac{(E_m \sin \theta)^2}{R} dt$$

$$\Rightarrow V^2 = \frac{\int_0^t (E_m \sin \theta)^2 dt}{t}$$

$$\Rightarrow V = \sqrt{\frac{\int_0^t (E_m \sin \theta)^2 dt}{t}}$$

$$\Rightarrow V = \sqrt{\int_0^t \frac{E_m^2 \sin^2 \theta}{t} dt}$$

$$\Rightarrow V = E_m \sqrt{\int_0^t \frac{\sin^2 \omega t}{t} dt}$$

$$\Rightarrow V = E_m$$

$$\Rightarrow E_{eff} = E_m \sqrt{\int_0^t \frac{\sin^2 \omega t}{t} dt}$$

$$\Rightarrow E_{eff} = E_m \sqrt{\int_0^t \frac{1 - \cos 2\omega t}{2} dt}$$

$$= \frac{E_m}{\sqrt{2}} \sqrt{\int_0^t \frac{1 - \cos 2\omega t}{t} dt}$$

$$= \frac{E_m}{\sqrt{2}} \sqrt{\int_0^t \frac{dt}{t} - \int_0^t \frac{\cos 2\omega t}{t} dt}$$

$$= \frac{E_m}{\sqrt{2}} \sqrt{\left[t - \frac{\sin 2\omega t}{2\omega} \right]_0^t}$$

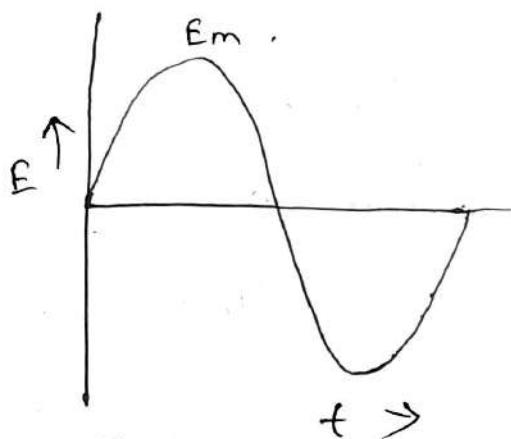
PEAK FACTOR

Peak factor of alternating quantity is ~~def~~ defined as the ratio between peak value to the effective value of the alternating quantity.

$$\text{Peak factor} = \frac{\text{peak value}}{\text{Effective value}}$$

$$\Rightarrow \text{Peak factor} = \frac{E_m}{\frac{E_m}{\sqrt{2}}}$$

$$\Rightarrow \sqrt{2} = 1.414$$



FORM FACTOR

Form factor of alternating quantity is defined as the ratio between effective ~~value~~ value to the average value of the alternating quantity.

$$\text{Form factor} = \frac{\text{Effective value}}{\text{Average value}}$$

$$= \frac{\frac{E_m}{\sqrt{2}}}{\frac{2E_m}{\pi}}$$

$$= \frac{\pi}{2\sqrt{2}} = \frac{22}{7} \times \frac{1}{2\sqrt{2}} = 1.11$$

(Q1):- The instantaneous value of current waveform is given by

$$I = 25 \sin 314t \text{ A. (i) calculate Peak current.}$$

(ii) - ~~Amplitude~~ ^{RMS} current.

(iii) - Average current. Given that

$$\text{Peak factor} = 1.414$$

$$\text{Form factor} = 1.1$$

Ans:-

$$I = I_m \sin \omega t$$

(i) Peak current (I_m) = 25 A.

$$\omega = 314 \text{ A.}$$

~~Peak current~~ I_m

$$(ii) \text{Peak factor} = \frac{I_m}{I_{rms}}$$

$$\Rightarrow 1.414 = \frac{25}{I_{rms}}$$

$$\Rightarrow I_{rms} = \frac{25}{1.414} = 17.68 \text{ A.}$$

(iii) -

$$\text{Form factor} = \frac{I_{rms}}{I_{avg}} = \frac{17.68}{I_{avg}}$$

$$\Rightarrow \frac{2.5}{\pi} = \frac{17.68}{I_{avg}}$$

$$\Rightarrow \frac{2E_m}{\pi} = 15.92$$

$$\Rightarrow 2E_m = 50.50$$

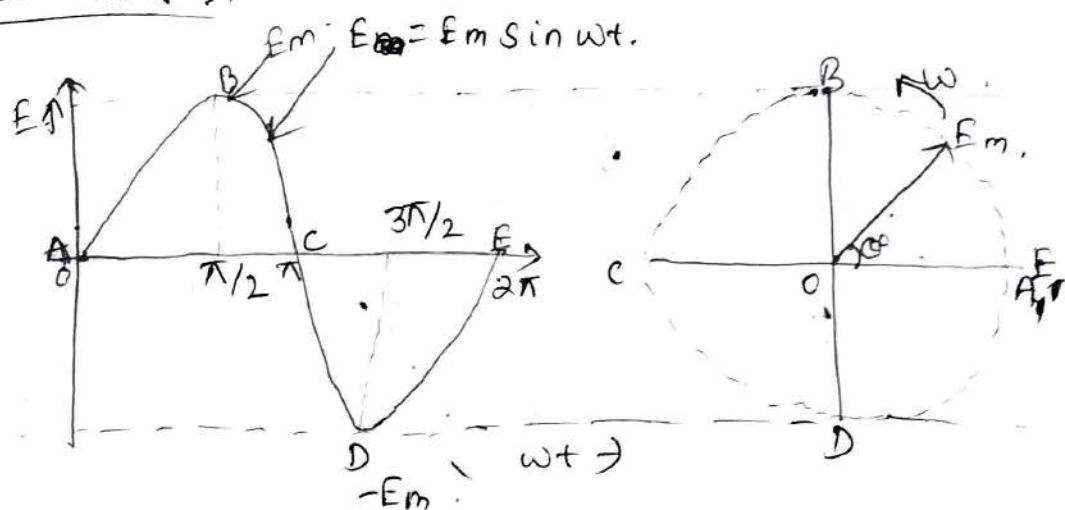
$$\Rightarrow E_m = \frac{50.50}{2} = 25.25$$

$$\Rightarrow I_{avg} = \frac{17.68}{1.11}$$

$$\Rightarrow I_{avg} = 15.92$$

Dt. 4.6.22

Sinusoidal waveform and phasor representation of EMF :-

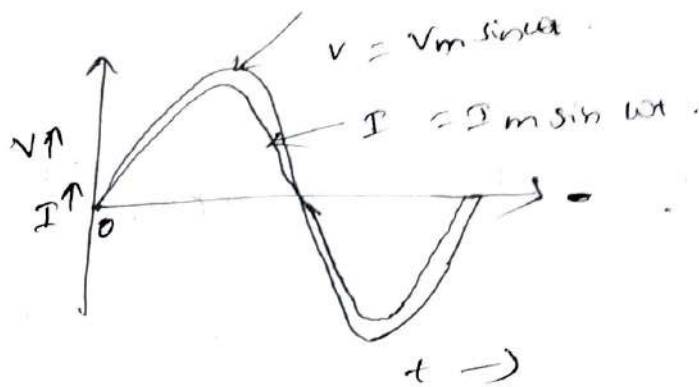


(waveform representation).

(phasor representation)

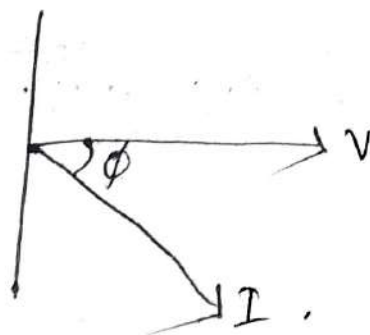
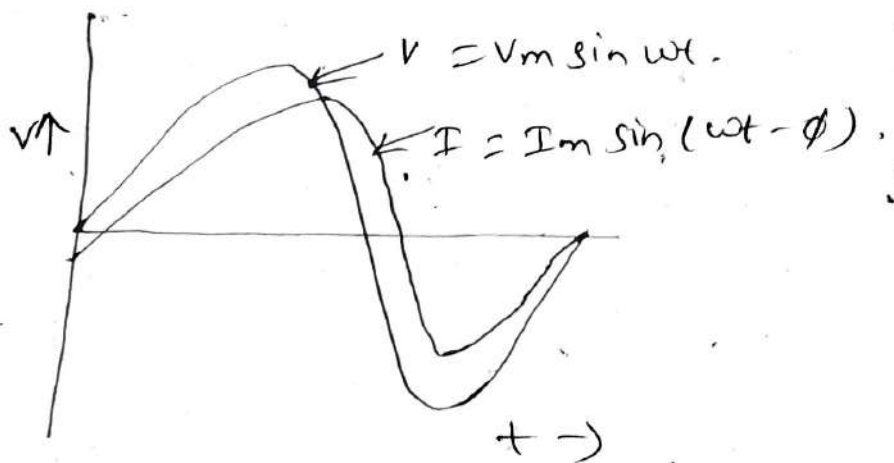
| Distance Point on waveform | Angular position of coil | Instantaneous EMF |
|----------------------------|--------------------------|-------------------|
| A | 0 | 0 |
| B | $\pi/2$ | E_m |
| C | π | 0 |
| D | $3\pi/2$ | $-E_m$ |
| E | 2π | 0 |

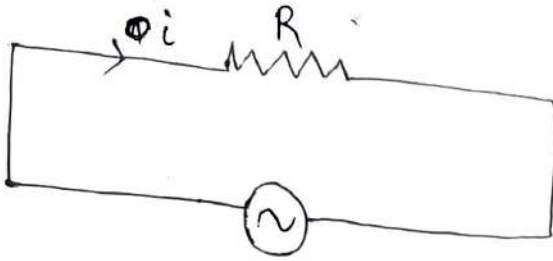
IN Phase:-



Two waveforms are said to be in ^(phase) phase if they begin simultaneously and end simultaneously.

Phase difference:-



~~Circuit containing~~Circuit containing Pure Resistance:-

$$V = V_m \sin \omega t.$$

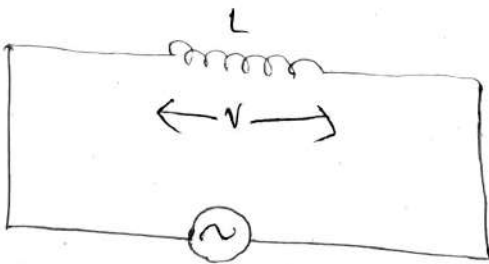
$$V = V_m \sin \omega t \quad \text{--- (1).}$$

$$I = \frac{V}{R} = \frac{V_m \sin \omega t}{R}.$$

$$\text{or } i = \frac{V_m}{R} \sin \omega t.$$

$$\therefore I = I_{\max} \sin \omega t. \quad \text{--- (2).}$$

$$\text{where } I_{\max} = \frac{V_m}{R}.$$

Circuit containing Pure Inductance:-

$$V = V_m \sin \omega t.$$

$$V = L \frac{dI}{dt}.$$

$$V = V_m \sin \omega t \quad \text{--- (1)}$$

$$V - V' = 0$$

$$\Rightarrow V' = V$$

$$\Rightarrow V' = V_m \sin \omega t$$

$$\Rightarrow L \frac{dI}{dt} = V_m \sin \omega t$$

$$\Rightarrow \frac{dI}{dt} = \frac{V_m}{L} \sin \omega t$$

$$\Rightarrow dI = \frac{V_m}{L} \sin \omega t dt$$

$$\Rightarrow \int dI = \frac{V_m}{L} \int \sin \omega t dt$$

$$\Rightarrow I = \frac{V_m}{L} \left\{ -\frac{\cos \omega t}{\omega} \right\}$$

$$\Rightarrow \frac{V_m}{\omega L} \left[\sin \left(-\frac{\pi}{2} + \omega t \right) \right]$$

$$= \frac{V_m}{\omega L} \left[\sin \left(\omega t - \frac{\pi}{2} \right) \right]$$

$$\Rightarrow \omega L = 2\pi f L = X_L$$

X_L = Inductive Reactance

unit = Ohm (Ω).

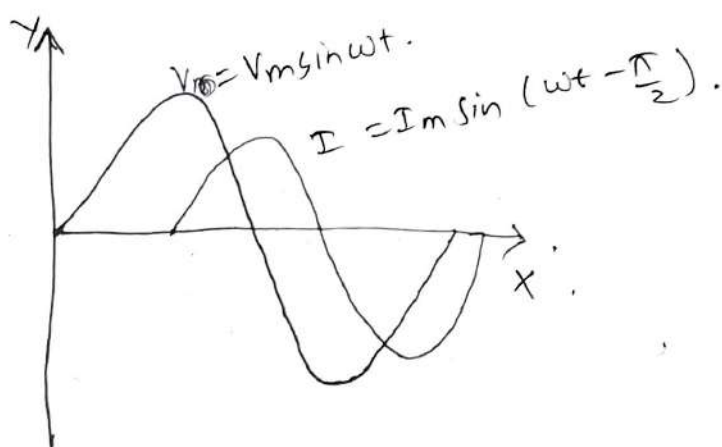
$$i = I_m \sin \left(\omega t - \frac{\pi}{2} \right) \quad \text{--- (2)}$$

where

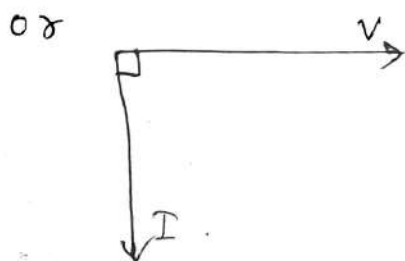
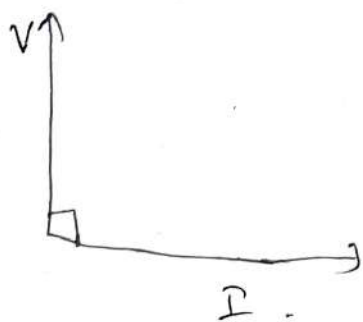
$$I_{\max} = \frac{V_m}{\omega L} \quad \text{or} \quad \frac{V_m}{X_L}$$

+ve sign \rightarrow Leading quantity.

ϕ -ve sign \rightarrow Lagging quantity.

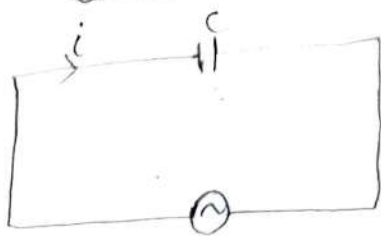


(Sinusoidal Representation)
or waveform



(Phasor Representation).

Circuit containing pure capacitance.



$$V = V_m \sin \omega t.$$

$$C = \frac{Q}{V}$$

unit = farad.

$$V = V_m \sin \omega t \quad \text{--- (1)}$$

$$Q = CV$$

$$i = \frac{dQ}{dt} = \frac{d}{dt} (CV)$$

$$i = C \frac{d}{dt} (V_m \sin \omega t)$$

$$= C V_m \omega \cos \omega t$$

$$i = C \omega V_m \cos \omega t$$

$$= C \omega V_m \sin \left(\omega t + \frac{\pi}{2} \right)$$

$$i = I_{\text{max}} \sin \left(\omega t + \frac{\pi}{2} \right) \quad \text{--- (2)}$$

$$\text{where } I_{\text{max}} = C \omega V_m$$

$$I_{\max} = \omega V_{\max}$$

$$\Rightarrow \frac{I_{\max}}{V_{\max}} = \omega$$

$$\Rightarrow \frac{V_{\max}}{I_{\max}} = \frac{1}{\omega}$$

$$\Rightarrow \frac{\frac{V_{\max}}{\sqrt{2}}}{\frac{I_{\max}}{\sqrt{2}}} = \frac{1}{\omega}$$

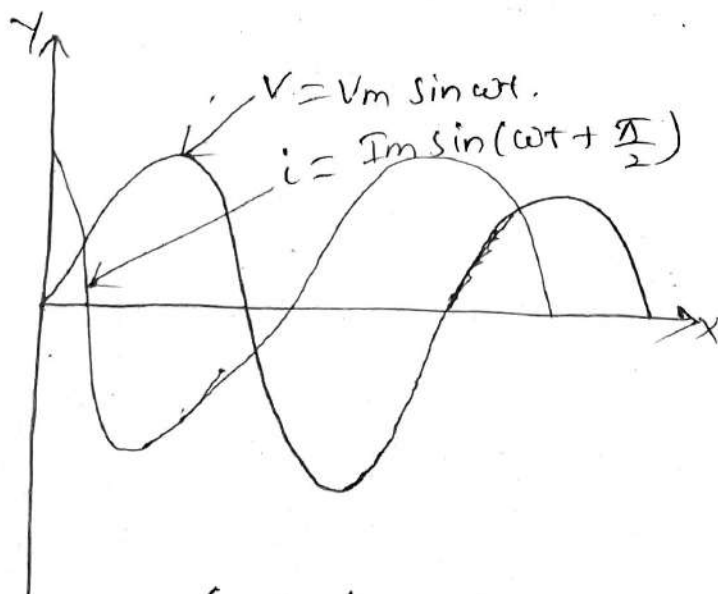
$$\text{or } \frac{V}{I} = \frac{1}{\omega} = X_C$$

$$\Rightarrow \frac{V}{I} = \frac{1}{2\pi fC}$$

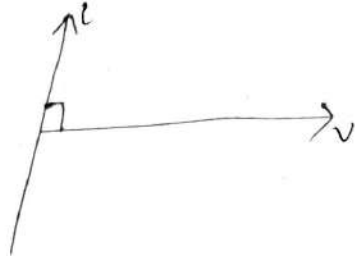
$$X_C = \frac{1}{2\pi fC}$$



capacitive Reactance.



(waveform Representation
(i))



(Phasor Representation).

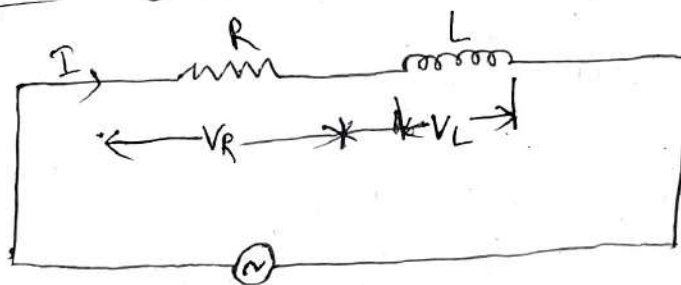
(ii).

$$R = \begin{array}{c} \xrightarrow{\quad} \\ \text{V} \quad \text{I} \end{array}$$

$$L = \begin{array}{c} \text{V} \\ \uparrow \\ \text{I} \end{array}$$

$$C = \begin{array}{c} \text{I} \\ \uparrow \\ \text{V} \end{array}$$

R.L. Series circuit :-



$$V = V_m \sin \omega t.$$

V_R = voltage across ~~resistor~~ Resistor. $= IR$.

V_L = voltage across Inductor. $= IX_L$.

I = current through the circuit.

Voltage Triangle



from Voltage Triangle,

$$V^2 = V_R^2 + V_L^2$$

$$\Rightarrow V^2 = (IR)^2 + (IX_L)^2$$

$$= I^2 R^2 + I^2 X_L^2$$

$$\Rightarrow V^2 = I^2 (R^2 + X_L^2)$$

$$\Rightarrow \frac{V^2}{I^2} = R^2 + X_L^2$$

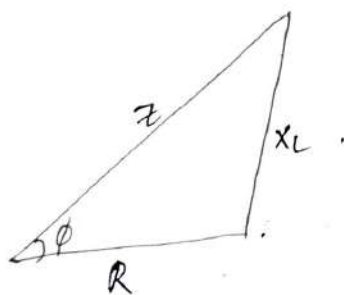
$$\Rightarrow \left[\frac{V}{I} = \sqrt{R^2 + X_L^2} \right]$$

$$\Rightarrow \left[Z = \sqrt{R^2 + X_L^2} \right]$$

$Z \rightarrow$ Impedance, Ω

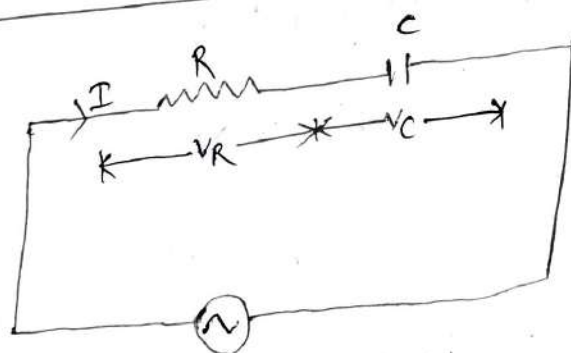
$$\text{Unit} = \text{ohm } (\Omega).$$

Impedance Triangle

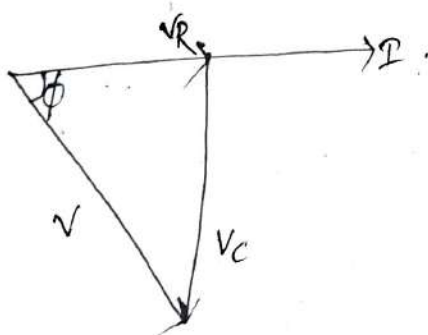


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RC series circuit



$V = V_m \sin \omega t$,
(circuit diagram).



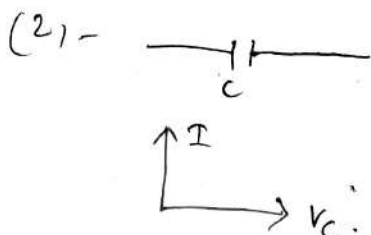
(Phasor Diagram).

V_R = voltage drop across Resistor

$$= IR.$$

V_c = voltage across capacitor = $I X_c$

I = circuit current.



from the triangle.

$$V^2 = V_R^2 + V_c^2$$

$$\Rightarrow V^2 = (IR)^2 + (IX_c)^2$$

$$= I^2 R^2 + I^2 X_c^2$$

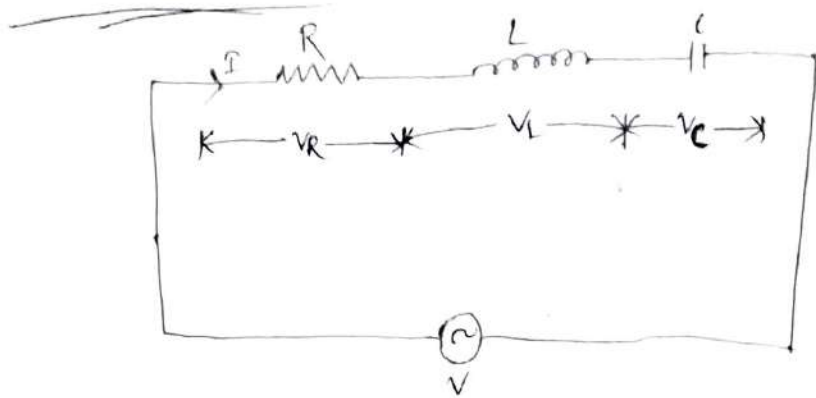
$$= I^2 (R^2 + X_c^2)$$

$$\Rightarrow \frac{V^2}{I^2} = R^2 + X_c^2$$

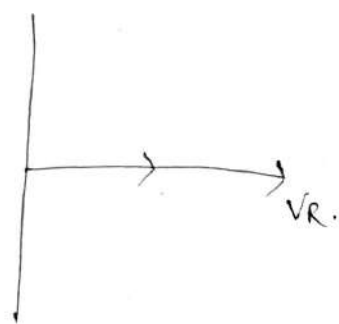
$$\Rightarrow \boxed{\frac{V}{I} = \sqrt{R^2 + X_c^2}}$$

$$\text{or } \boxed{Z = \sqrt{R^2 + X_c^2}}$$

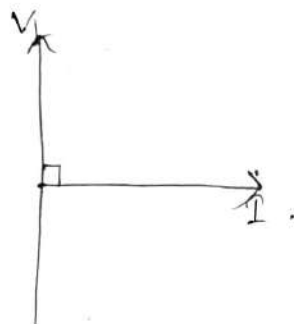
RLC series circuit:



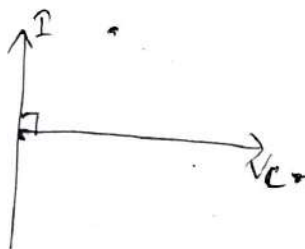
(Circuit diagram).



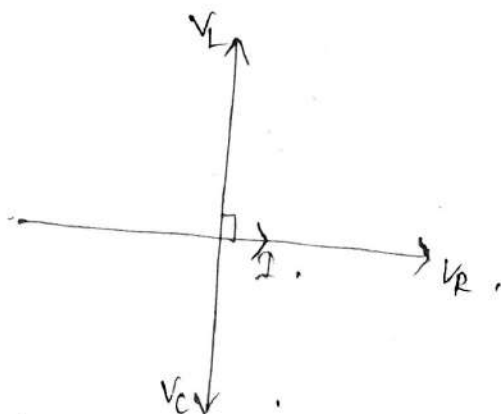
($V_R \propto I$).
(i).



($V_L \propto I$).
(ii).

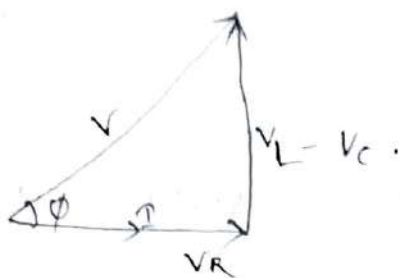


($V_C \propto I$).
(iii).



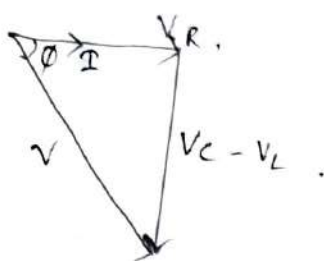
($V_R, V_L, V_C \propto I$).

Voltage Triangle :-



$$(X_L > X_C)$$

(i) :-



$$(X_L < X_C)$$

(ii) :-

From triangle

$$V^2 = V_R^2 + (V_L - V_C)^2$$

$$= (IR)^2 + (IX_L - IX_C)^2$$

$$= I^2 [R^2 + (X_L - X_C)^2]$$

$$\Rightarrow \frac{V^2}{I^2} = R^2 + (X_L - X_C)^2$$

$$\text{or } \frac{V}{I} = \sqrt{R^2 + (X_L - X_C)^2}$$

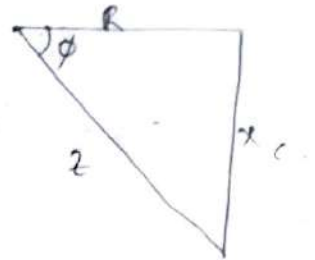
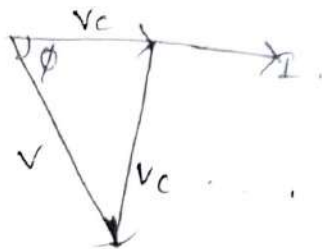
$$Z = \sqrt{R^2 + (X_L - X_C)^2}$$

$$(X_L > X_C)$$

$$Z = \sqrt{R^2 + (X_L - X_C)^2}$$

$$(X_L < X_C)$$

Impedance Triangle for RC circuit:



(Impedance Triangle)

$$V_R = IR / I = R$$

$$V_C = I X_C / I$$

$$= X_C$$

$$V/I = Z$$

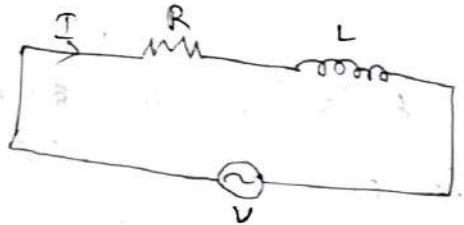
$$Z = \sqrt{R^2 + X_C^2}$$

(1) - A Series R.L. circuit having $R = 20 \Omega$, $L = 0.05 \text{ H}$ is connected across 100 V , 50 Hz supply. Calculate circuit current and power consumed.

$$R = 20 \Omega$$

$$L = 0.05 \text{ H}$$

$$V = 100 \text{ V}, 50 \text{ Hz}$$



$$I = \frac{V}{Z}$$

Z = impedance.

$$Z = \sqrt{R^2 + X_L^2}$$

$$X_L = 2\pi fL$$

$$= 2\pi \times \frac{22}{7} \times 50 \times 0.05$$

$$= \frac{22}{7} \times 50 \times \frac{5}{100}$$

$$= 15.7 \Omega$$

$$\begin{array}{r} 15.25 \\ 110 \\ \hline 7 \end{array}$$

$$Z = \sqrt{R^2 + (X_L)^2}$$

$$= \sqrt{20^2 + (15.7)^2}$$

$$= \sqrt{400 + 246.49}$$

$$= \sqrt{646.49}$$

$$= 25.4 \Omega$$

$$I = \frac{V}{Z}$$

$$I = \frac{100}{25.4} = \frac{1000}{254} = 3.93 \text{ A}$$

$$P = VI \cos \phi$$

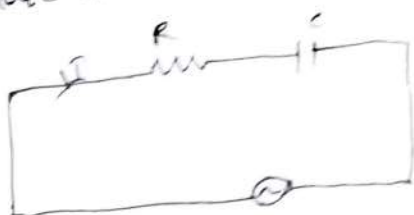
$$\cos \phi = \frac{R}{Z}$$

$$\Rightarrow P = 100 \times 3.93 \times \frac{R}{Z}$$

$$= 100 \times 3.93 \times \frac{20}{25.4}$$

$$= 309.4 \text{ W} \quad (\text{Ans})$$

(2) - A series RC circuit at ~~resistor~~ resistance
 $R = 20 \Omega$, $C = 125 \mu\text{f}$; a $V = 200\text{V}$, 50Hz is
 applied in the circuit. calculate V_R and V_C .



Ans:- $R = 20 \Omega$

$$C = 125 \mu\text{f}$$

$$V = 200\text{V}, 50\text{Hz}$$

$$V_R, V_C = ?$$

$$V_R = IR, \quad I = \frac{V}{Z}$$

$$Z = \sqrt{R^2 + X_C^2}$$

$$X_C = \frac{1}{2\pi fC}$$

$$= \frac{1}{2\pi \times 50 \times 125 \times 10^{-6}}$$

$$= 25.47$$

$$Z = \sqrt{R^2 + (25.47)^2}$$

$$I = \frac{V}{Z}$$

$$= \sqrt{20^2 + 648.72}$$

$$= \sqrt{400 + 648.72}$$

$$= \sqrt{1048.72} = 32.38$$

$$I = \frac{V}{Z} = \frac{200}{32.38} = 6.18 \text{ A}$$

$$V_R = I \times R = 6.18 \times 20 = 123.6 \text{ V}$$

$$V_C = I X_C$$

$$X_C = \frac{1}{2\pi fC}$$

$$=$$

$$I = \frac{V}{Z} = \frac{200}{25.42}$$

$$I = 7.87 \text{ A}$$

$$V_R = I \times R$$

$$= 6.17 \times 20$$

$$= 123.4$$

$$V_L = I \times X_L$$

$$= 6.17 \times 25.42$$

$$= 157.4 \text{ V, (Ans)}$$

(3) - A series RLC circuit having resistance $(R) = 10 \Omega$, $L = 0.2 \text{ H}$, $C = 100 \mu\text{F}$ is connected across 100 V , 50 Hz supply. Calculate current and Power factor.

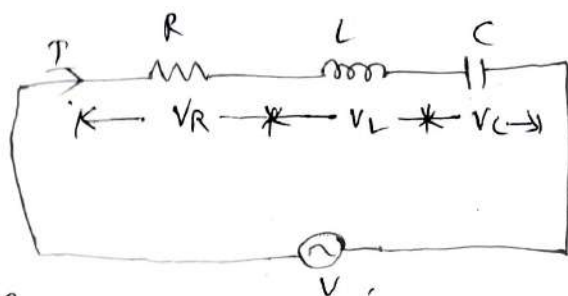
Ans.

$$R = 10 \Omega$$

$$L = 0.2 \text{ H}$$

$$C = 100 \mu\text{F}$$

$$V = 100 \text{ V, } 50 \text{ Hz} = 100 \times 10^6$$



$$I = \frac{V}{Z}$$

$$Z = \sqrt{R^2 + (X_L - X_C)^2}$$

$$Z = \sqrt{R^2 + (X_C - X_L)^2}$$

$$X_L = 2\pi fL$$

$$= 2 \times \frac{22}{7} \times 50 \times 0.2$$

$$= 62.85 \Omega$$

$$X_C = \frac{1}{2\pi fC}$$

$$= \frac{1}{2 \times \frac{22}{7} \times 50 \times 100 \times 10^{-6}}$$

$$= 31.8 \Omega$$

$$Z = \sqrt{R^2 + (X_L - X_C)^2}$$

$$= \sqrt{10^2 + (31.7)^2}$$

$$= 32.57 \Omega$$

$$Q = \cancel{31.7}$$

$$I = \frac{V}{Z} = \frac{100}{32.57} = 3.07 \text{ A}$$

$$\text{Power factor (P.f.)} = \cos \phi = \frac{R}{Z}$$

$$= \frac{100}{32.57}$$

$$= 0.307$$

(Ans)

04.7.22

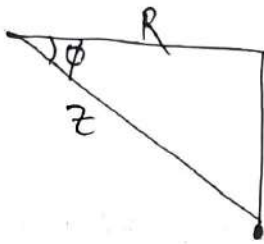
Impedance triangle for RLC series circuit :-



$$X = X_L - X_C.$$

$$(X_L > X_C)$$

(i).



$$X = X_C - X_L.$$

$$(X_C > X_L)$$

(ii).

X = Net reactance.

$$Z = R \pm jX.$$

R = Resistance.

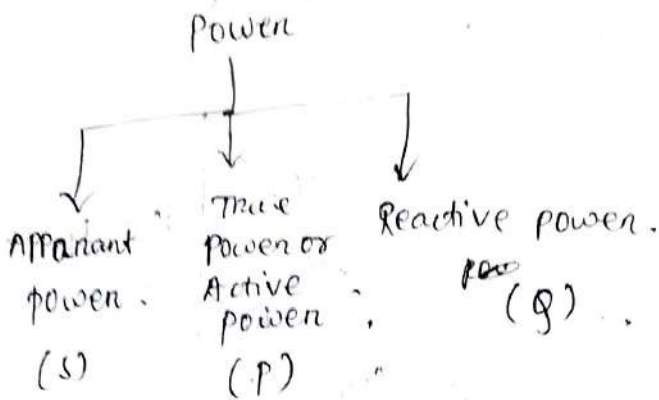
$$Z = R + jX$$

$$(X_L > X_C).$$

$$Z = R - jX$$

$$(X_C > X_L).$$

Power and Power factor:-



Apparent power (S) :-

$$S = VI$$

unit = volt Ampere (VA)

The product of RMS value of voltage and current is called apparent power and it is measured in Volt Ampere or KVA.

True power (P) :-

$$P = VI \cos \phi$$

unit = watt or kW

The true power is obtained by multiplying the apparent power by power factor, and it is measured in W or kW.

Reactive power (Q) :-

$$Q = VI \sin \phi$$

unit = Reactive volt Ampere (VAR)

The product of apparent power and sine of the angle between voltage and current is called reactive power and it is measured in Reactive volt Ampere (VAR).

$$P = VI \cos \phi$$

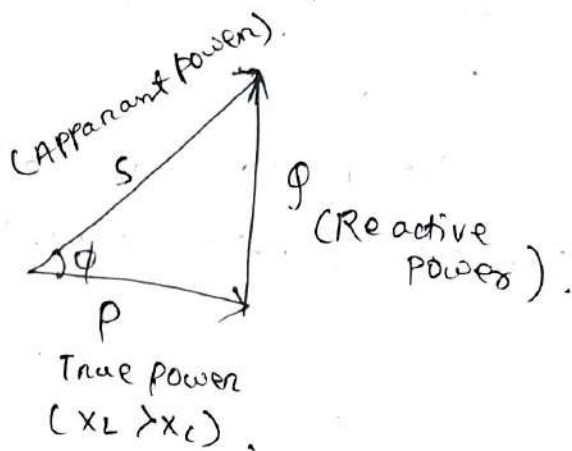
$$\cos \phi = \frac{P}{VI}$$

① - It is the cosine of the angle betw voltage and current.

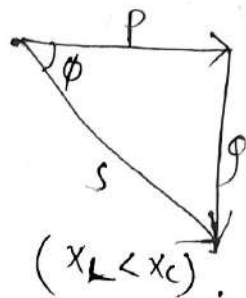
② - It is the ratio betw resistance and Inductan Impedence.

③ - It is the ratio betw true power and appanant power.

Power triangle:



(i).



$$S = P \pm jQ$$

S = Appanant power.

P = True power or ~~Act~~ Active power.

Q = Reactive power.

$$S = P + jQ \quad (x_L > x_C)$$

$$S = P - jQ \quad (x_L < x_C)$$

$$|S| = \sqrt{P^2 + Q^2}$$

(Q): An RL series circuit contains a

~~Res~~ $R = 5 \Omega$, $L = 50 \text{ mH}$, $C = 400 \mu\text{F}$

Draw the impedance triangle for the circuit when a sinusoidal voltage,

50 Hz. (i) Express the impedance in the complex form.

(ii) - what is the phase angle between the voltage and current for the circuit.

Ans:- $R = 5 \Omega$.

$L = 50 \text{ mH}$.

$C = 400 \mu\text{F} = 4 \times 100 \times 10^{-6}$.

$\omega = 50 \text{ Hz}$.

$$X_C = \frac{1}{2\pi fC}$$

$$= \frac{1}{2 \times \frac{22}{7} \times 4 \times 100 \times 10^{-6} \times 50}$$

$$= 7.95 \Omega$$

$$X_L = 2\pi fL$$

$$= 2 \times \frac{22}{7} \times 50 \times 50 \times 10^{-3}$$

$$= 15.9 \, \Omega$$

$$X_L > X_C$$

$$X = X_L - X_C = 15.9 - 7.9$$

$$= 7.8$$

$$(i) - Z = R + jX$$

$$= 5 + j \times 7.8$$

$$|Z| = \sqrt{5^2 + (7.8)^2} = 9.26$$

$$(ii) - \cos \phi = \frac{R}{Z} = \frac{5}{9.26} \quad \text{--- (Ans) ---}$$

$$\phi = \cos^{-1} \left(\frac{R}{Z} \right)$$

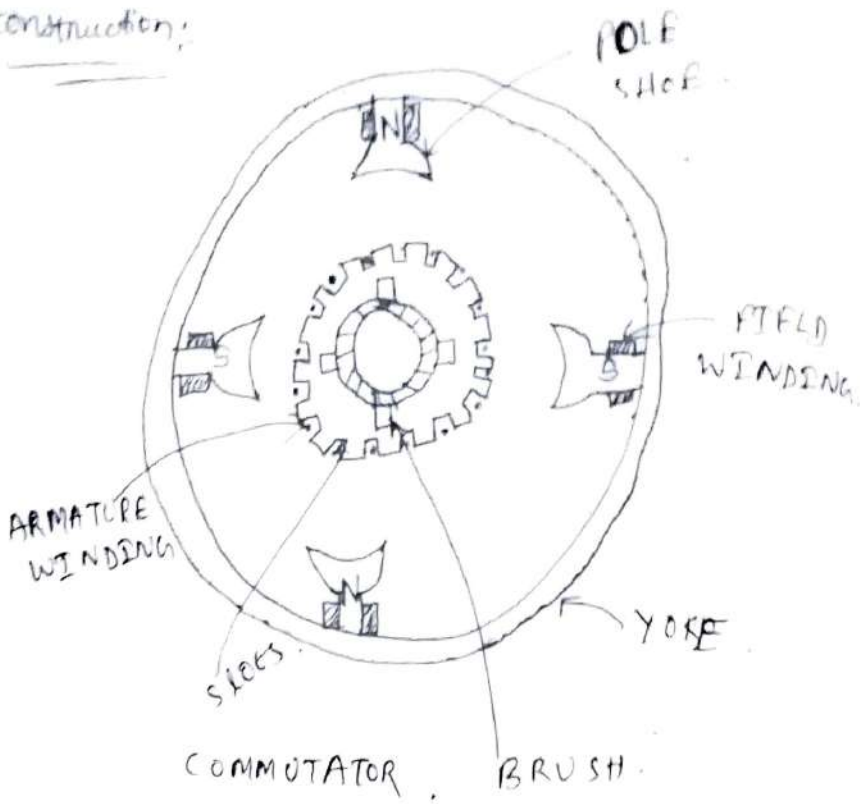
$$= \cos^{-1} \left(\frac{5}{9.26} \right)$$

$$= \cos^{-1} \left(\frac{5}{9.26} \right)$$

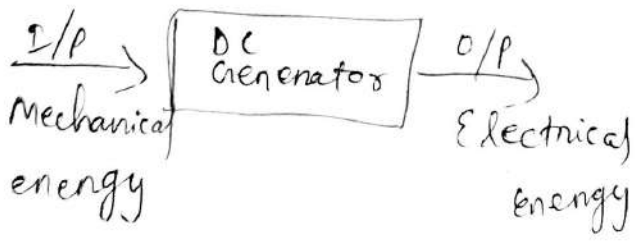
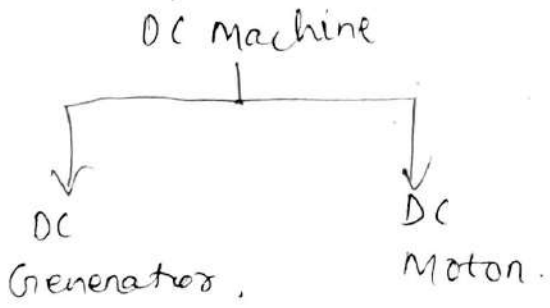
$$= 57.34^\circ \text{ (Ans) }$$

Dc Generator

construction:



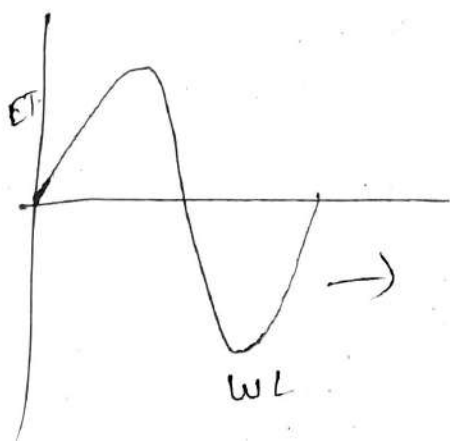
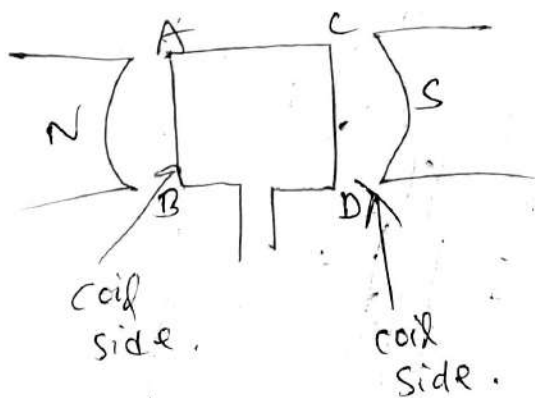
Dc machine :-



construction:-

- (1) - Yoke.
- (2) - Field winding.
- (3) - Pole core and pole shoe.
- (4) - Armature core.
- (5) - Armature winding.
- (6) - Commutator.
- (7) - Brush.

- (1) - Lap winding.
- (2) - wave winding.



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EMF equation of DC generator.

Let $P = 12$ poles.

ϕ : flux per pole in wb.

Z : Total no. of armature conductors.

N : No. of armature rev. in 1 min.

A : No. of parallel paths. (revolution per minute)

$A = P$ --- for lap winding.

$A = \frac{P}{2}$ --- for wave winding.

Flux cut by one conductor in one revolution at armature.

$$d\phi = P\phi \text{ wb.}$$

Time taken to complete one revolution.

$$dt = \frac{60}{N} \text{ sec.}$$

$$N \text{ rev} = 60 \text{ s.}$$

$$1 \text{ rev} = \frac{60}{N} \text{ sec.}$$

EMF generated per conductor

$$e = \frac{d\phi}{dt}$$

$$= P\phi$$

$$\frac{\frac{P\phi}{60}}{N} = \frac{P\phi N}{60} \text{ volt.}$$

EMF of Generator = $\frac{\text{Emf per conductor} \times \text{No. of conductors in series per parallel path}}{\text{conductor}}$

$$= \frac{P \Phi N}{60} \times \frac{Z}{A}$$

$$E_g = \frac{P \Phi Z N}{60 A}$$

(Q1) A 6 pole lap on DC Generator at 600 rpm
 cuts armature. The flux per pole is 0.02 Wb.
 calculate

(i) the speed at which the generator must
 be run to generate 300 volt.

(ii) what would be the speed if the
 generator were ~~not~~ wave wound.

$$P = 6 = A$$

$$Z = 600$$

$$\Phi = 0.02 \text{ Wb}$$

$$E_g = 300 \text{ V}$$

$$E_g = \frac{P \Phi Z N}{60 A}$$

Types of DC Generator:

sepa
Separately excited
DC generator.

self excited
DC generator.

Series
Generator.

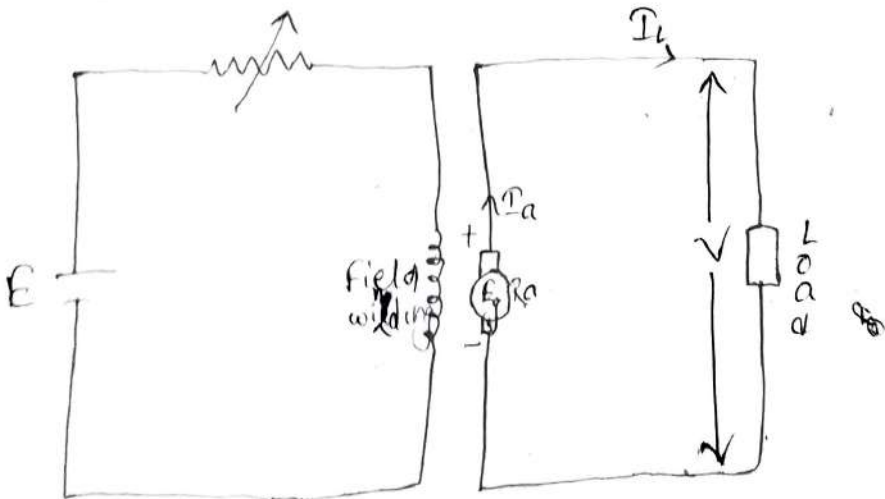
Shunt
Generation.

Compound
Generator.

Long
shunt.

Short
shunt.

(1) - Separately excited DC generator:



$$I_a = I_L$$

$$E_g - I_a R_a - V = 0$$

$$\boxed{E_g = V + I_a R_a}$$

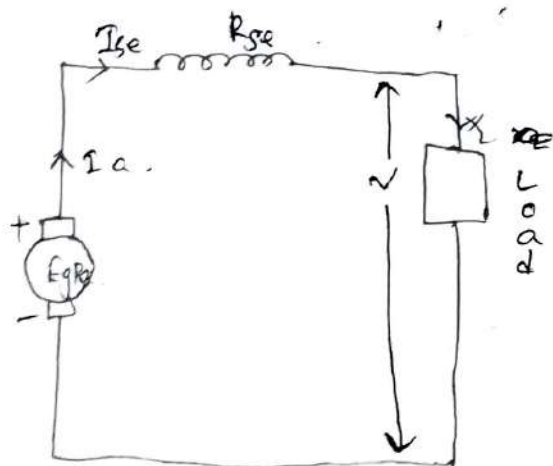
Power developed by the Armature.

$$E_g \times I_a = E_g I_a.$$

Power developed to load = $V I_L$.

(2)- Self Excited Dc Generator:-

(i)- Series Generator:-



$$I_a = I_{se} = I_L$$

$$= I$$

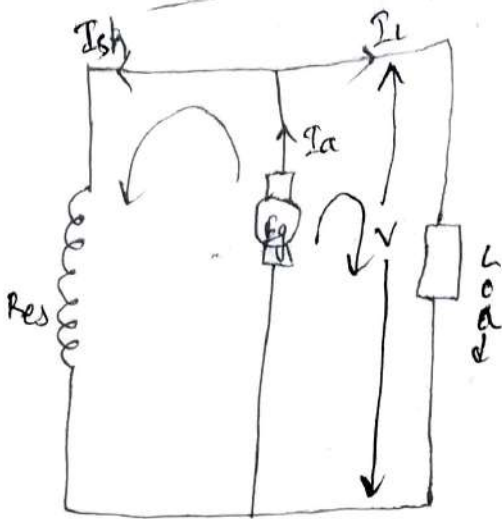
~~E_g~~

$$E_g - I_a R_a - V - I_{se} R_{se} = 0.$$

$$\Rightarrow E_g - I (R_a + R_{se}) - V = 0.$$

$$\Rightarrow \boxed{E_g = V + I (R_a + R_{se})}$$

(ii) - Shunt Generator:-



$$I_a = I_L + I_{sh}$$

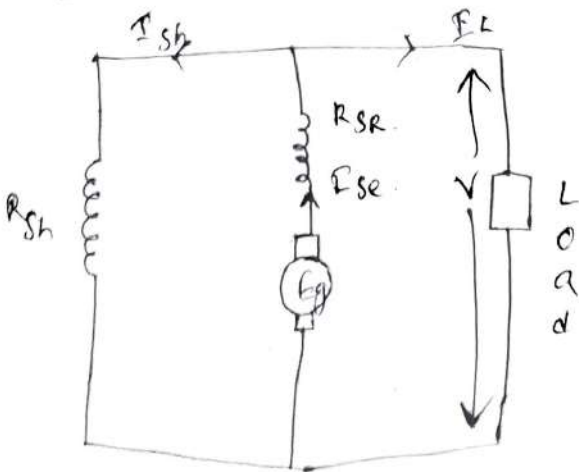
$$I_{sh} = \frac{V}{R_{sh}}$$

$$E_g - I_a R_a - V = 0$$

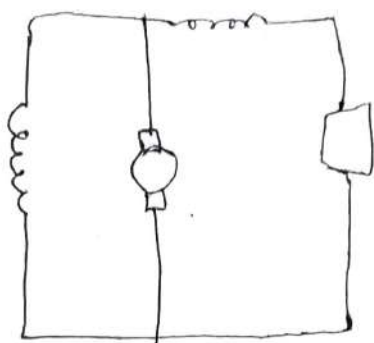
$$\text{or } E_g = V + I_a R_a$$

Compound Generator:-

(i) - Long shunt:-



(ii) - short shunt :-



Principle of Generators:

- * An electric Generator is a Machine that convert mechanical energy to electrical energy.
- * An electric Generator is based on the principle that whenever flux is cut by a conductor, ^{an emf is} induced which will cause a current to flow if the conductor's circuit is closed.

* Consider a single turn loop ABCD rotating in clock wise in a uniform magnetic field with a constant speed. As the loop rotate, the flux ~~link~~ linking the coil sides AB & ~~CD~~ CD changes continuously.

(i) - When the loop is in Position No-1 the generated emf is zero because the coil side AB & CD are cutting no flux but are moving parallel to it.

(ii) - When the loop is in position No-2 the coil sides ~~are~~ ~~are~~ are ~~more~~ moving at an angle to the flux and therefore ~~therefore~~ a low emf is generated.

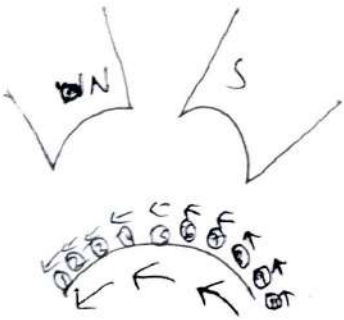
(iii) - When the loop is in position no. - 3 the coil sides are at right angled angle to the flux and therefore cutting the flux is at a maximum rate. Hence at this instant the generated emf is 'maximum'.

(iv) - At position - 4 the generated emf is less because the coil sides are cutting the flux at an angle.

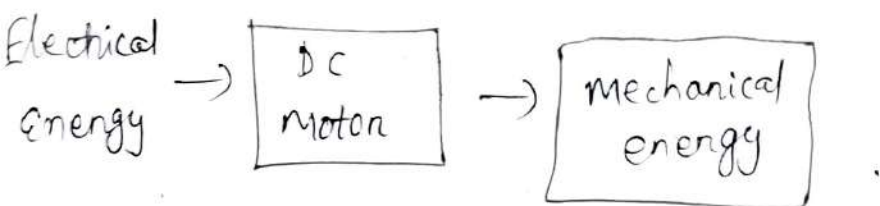
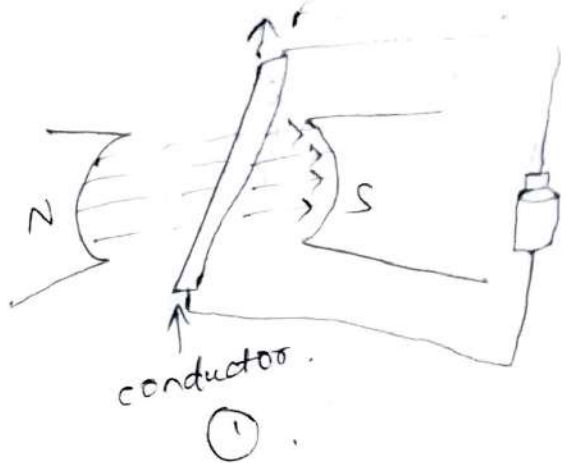
(v) - At position - 5 no magnetic lines are cut and hence induced emf is zero.

(vi) - At position - 6 the coil sides move under a pole of opposite polarity and hence the dirⁿ of generated emf is reversed.

(vii) - The max^m emf in the reverse dirⁿ will be when the loop is at position - 7. This cycle repeats with its revolution of the coil.

Principle:-

(1)



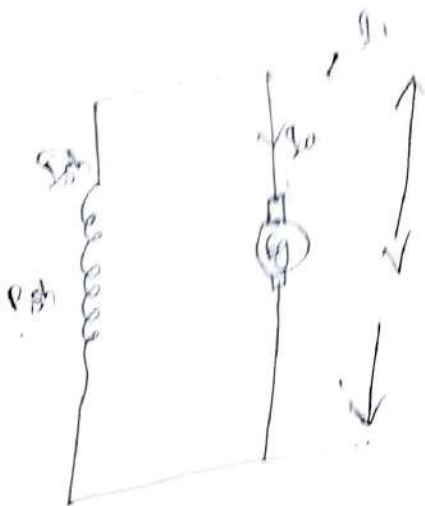
When a current carrying ~~con~~ conductor is placed in a magnetic field it will experience a mechanical force.

$$F = B i l \text{ Newton.}$$

B = Flux density.

i = current of the conductor.

L = length of the conductor.



$$I_L = I_a + I_{sh}$$

$$E_b = \text{Back EMF}$$

Net voltage across armature circuit.
 $= V - E_b$

1b

1b R_a is Armature resistance.

$$I_a = \frac{V - E_b}{R_a}$$

$$\text{or } I_a R_a = V - E_b$$

$$\boxed{E_b = V - I_a R_a}$$

$$\boxed{E_b = \frac{P \phi Z N}{60 A}}$$

Speed Equation of DC motor :

$$E_b = V - I_a R_a \quad \text{--- (1)}$$

$$E_b = \frac{P \phi Z N}{60 A} \quad \text{--- (2)}$$

$$\frac{P \phi Z N}{60 A} = V - I_a R_a$$

$$N = \frac{V - I_a R_a \times 60 A}{P \phi Z}$$

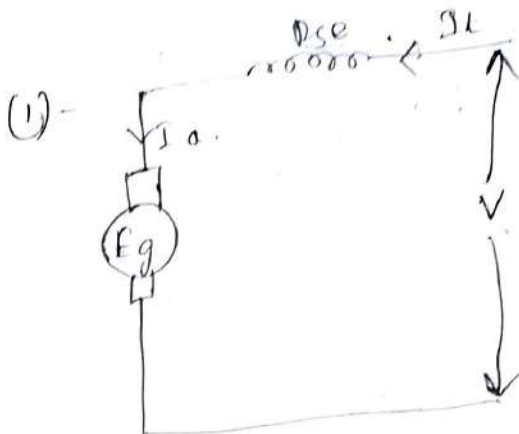
$$\Rightarrow N = \frac{V - I_a R_a}{\phi} \times \frac{60 A}{P Z}$$

$$\Rightarrow N = \frac{E_b}{\phi} \cdot K \quad \left(\frac{60 A}{P Z} = K \right)$$

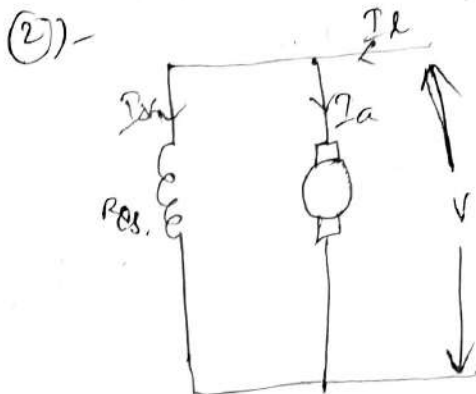
$$\Rightarrow \boxed{N \propto \frac{E_b}{\phi}}$$

Types of DC MOTOR:

- (1) - series motor.
- (2) - shunt motor.
- (3) - compound motor.

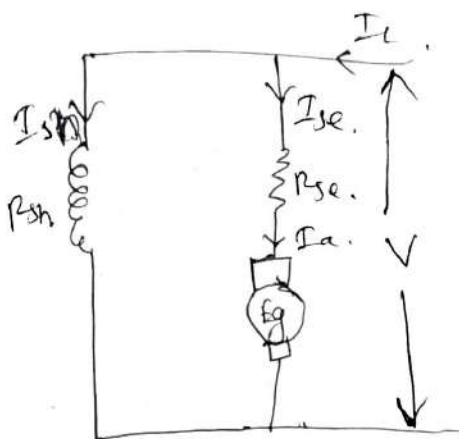


$$I_L = I_{se} = I_a$$

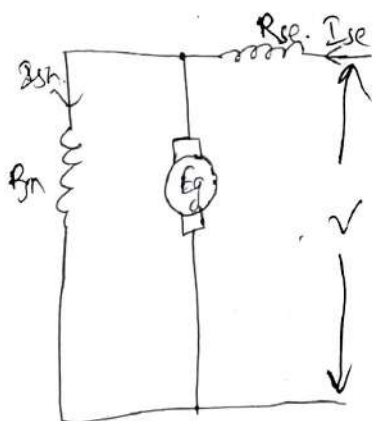


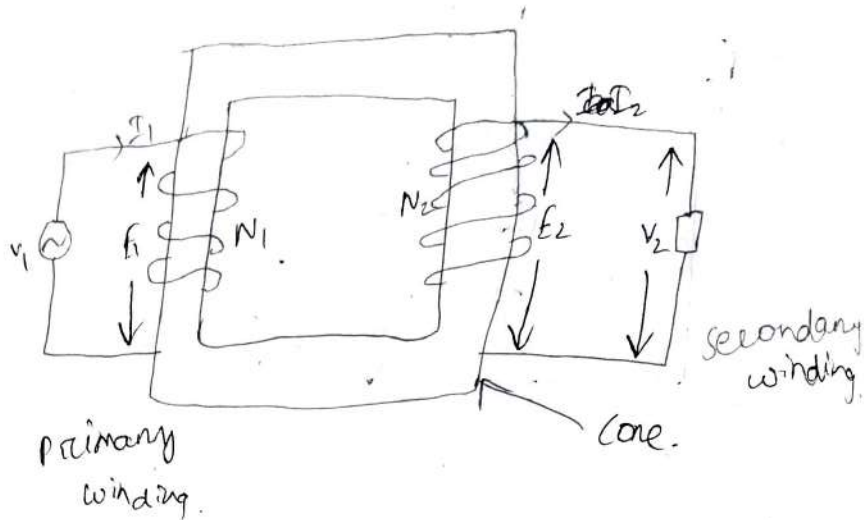
$$I_L = I_a + I_{sh}$$

317 long shunt , -



318 short shunt :-





$$E_1 = -N_1 \frac{d\phi}{dt}$$

$$E_2 = -N_2 \frac{d\phi}{dt}$$

$$\frac{E_2}{E_1} = \frac{N_2}{N_1}$$

If $V_2 > V_1 \rightarrow$ step up Transformer.

$V_2 < V_1 \rightarrow$ step down Transformer.

Transformation Ratio (K) :-

$$\frac{V_2}{V_1} = \frac{N_2}{N_1} = K.$$

For Ideal Transformer.

$$\frac{V_2}{V_1} = \frac{N_2}{N_1} = \frac{E_2}{E_1} = K.$$

Ideal transformer :-

(1) - No winding resistance.

(2) - No Iron loss.

(3) - No leakage reactance.

EMF eqⁿ of Transformer :-

The sinusoidal flux produced in the primary.

$$\phi = \phi_m \sin \omega t.$$

The instantaneous emf produced in the primary.

$$E = -N_1 \frac{d\phi}{dt}.$$

$$e_1 = -N_1 \frac{d\phi}{dt} (\phi_m \sin \omega t)$$

$$= -\omega N_1 \phi_m \cos \omega t$$

$$\Rightarrow \omega = 2\pi f$$

$$= -2\pi f N_1 \phi_m \cos \omega t$$

$$e_1 = 2\pi f N_1 \phi_m \sin \left(\omega t - \frac{\pi}{2} \right)$$

The maximum value of induced emf in the primary.

$$E_{\text{max}} = 2\pi f N_1 \phi_m$$

The r.m.s value of induced emf in the primary.

$$= \frac{E_m}{\sqrt{2}} = \frac{2\pi f N_1 \phi_m}{\sqrt{2}}$$

$$E_2 = 4.44 f \phi_m N_2$$

$$E_1 = 4.44 f \phi_m N_1$$

Construction of Transformer:

Two main parts of a single phase Transformer are

- (i) - A set of two isolated winding.
- (ii) - A common magnetic ~~winding~~ core.

Depending on the winding arrangement over the core.

Transformer may be classified ~~types~~ as

- (i) - core type
- (ii) - shell type.

1) In core type transformer the winding surround the core.

2) ~~The~~ In shell type transformer the core surround the winding.

3) The core is provided to localize the magnetic flux for linking the two windings.

4) Therefore the core is made up of highly permeable magnetic material.

5) The core is also laminated to reduce Eddy current loss.

6) The windings are made up of highly conducting material in the form of copper wire having an enamel coating on their surface which provides the necessary insulation for isolation of the winding from remaining conducting parts of the transformer.

→ Thus the two windings remain electrically isolated from one another.

→ On the other hand both windings being placed on a common magnetic core established a mutual linkage with the common magnetic flux.

→ Hence ~~the~~ the ~~two~~ two windings ~~are~~ remain magnetically coupled.

→ Among the auxiliary parts there is an enclosed tank houses total core and winding assembly.

→ The core and winding assembly remain completely built & immersed in a transformer ~~grade~~ grade mineral oil.

→ The free end of the winding are ~~brought~~ brought out of the tank through a special type of insulation mounting called bushing and terminals are provided at the top of bushing to enable external connection.

Power Billing

dt. 25.7.22

Q1:- A building has the following electrical

(i) - 1 H.P motor running for 5 Hours in a day.

(ii) - 3 fans each of 80 watt running for 10 hours in a day.

(iii) 4 tube lights of 40 watt running for 15 hours per day.

Find the monthly bill for the month of November of 2021. 16 ~~index~~ unit. cost of bill is RS 2.50.

| S.No. | Name of Appliances | quantity | power rating | working hours in a day | Energy consumed in KWH. |
|-------------------------------|--------------------|----------|---------------|------------------------|---|
| 1- | motor | 1 No | 1 H.P = 746w. | 5 | $\frac{746 \times 5 \times 1}{1000} = 3.73$ |
| 2- | fan | 3 No | 80w. | 10 | $\frac{80 \times 3 \times 10}{1000} = 2.4$ |
| 3 | Tubelight | 4 No | 40w | 15 | $\frac{15 \times 40 \times 4}{1000} = 2.4$ |
| Total energy consumed per day | | | | | $= 3.73 + 2.4 + 2.4$ |
| | | | | | $= 8.53 \text{ Kw}$ |

In the month of November is 30 days.

So $30 \times 8.53 = 255.9 \text{ KWH}$.

Total cost of energy

1500 units \times cost per unit

250 \times 2.5

RS 639.75.

(Ans)

(Q) Find the cost of electrical energy in the month of January 2022 in a residential house, each unit of energy cost RS 2.50.

(i) - 5, 60w lamps for 8 hours.

(ii) - 3, 100w ceiling fans for 6 hours.

(iii) - 4, 40 watt fluorescent tubelight for 4 hours.

| Sl No | Name of Appliances | Quantity | Power rating | Working hours in a day | Energy consumed |
|--------------------------------|--------------------|----------|--------------|------------------------|--|
| 1 | Lamps | 5 No | 60w | 8 | $\frac{60 \times 8 \times 5}{1000} = 2.4$ |
| 2 | 8 fans | 3 No | 100w | 6 | $\frac{100 \times 6 \times 3}{1000} = 1.8$ |
| 3 | tubelight | 4 No | 40w | 4 | $\frac{40 \times 4 \times 4}{1000} = 0.64$ |
| Total energy consumed per day. | | | | | $2.4 + 1.8 + 0.64$ |
| | | | | | $= 4.84$ |

In the month of January of 2022 is 31 day

$$\begin{aligned} \text{So } &= 31 \times 4.84 \\ &= 150.04 \text{ kWh} \end{aligned}$$

Total cost of Energy

$$= \text{No. of units} \times \text{cost per unit}$$

$$= 150.04 \times 2.50$$

$$= \text{Rs } 375.10 \dots \underline{\underline{(\text{Ans})}}$$